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**STATIC STABILITY AND MAGNUS CHARACTERISTICS OF THE U. S. NAVY 1,000
POUND LOW - DRAG BOMB AT TRANSONIC SPEEDS**

**FC
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5 APRIL 1957



**U. S. NAVAL ORDNANCE LABORATORY
WHITE OAX, MARYLAND**

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Aeroballistic Research Report 345

STATIC STABILITY AND MAGNUS CHARACTERISTICS OF THE
U. S. NAVY 1,000 POUND LOW-DRAG BOMB AT
TRANSONIC SPEEDS

Prepared by:

J. E. Greene

ABSTRACT: The Magnus and static stability characteristics of a 0.214-scale model of the U. S. Navy 1,000 pound Low-Drag Bomb have been obtained from transonic wind-tunnel tests at angles of attack up to 22 degrees and for various free-stream Reynolds numbers. The variation in static aerodynamic coefficients due to roll orientation of the bomb through the range 0 - 180 degrees and drag effects due to the addition of external mounting lugs were also investigated. The tests were conducted by NOL in the Cornell Aeronautical Laboratory 4 x 3 foot transonic test facility.

The results of the test indicate that the Magnus characteristics of the bomb are linear with rotational speed and non-linear with angle of attack. Variation in the free-stream Reynolds number is seen to affect the measured Magnus characteristics appreciably at all Mach numbers and angles of attack. It is further shown that significant changes in the pitch, yaw, and roll moments may be expected to accompany variations in the roll orientation of the bomb.

U. S. NAVAL ORDNANCE LABORATORY
WHITE OAK, MARYLAND



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5 April 1957

This report presents the Magnus and static stability characteristics of a 0.214-scale model of the U. S. Navy 1,000 pound Low-Drag Bomb at transonic speeds. The data were obtained in the 4 x 3 foot transonic test facility at the Cornell Aeronautical Laboratory in Buffalo, New York under task number 803-767/73003/01. Special instrumentation required to spin the model and measure dynamic forces and moments was furnished by the Naval Ordnance Laboratory.

W. W. WILBOURNE
Captain, USN
Commander

H. H. KURZWEG
By direction

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STATIC STABILITY AND MAGNUS CHARACTERISTICS OF THE
U. S. NAVY 1,000 POUND LOW-DRAG BOMB AT
TRANSONIC SPEEDS

INTRODUCTION

1. The Low-Drag Bomb family stems from an external-store design originally developed by the Douglas Aircraft Company. The bombs of the series are geometrically similar in shape but vary in weight from 250 pounds (Mk 79) to 2,000 pounds (Mk 82). For the purpose of the investigation reported herein, the 1,000 pound bomb, Mk 81, has been chosen as the representative bomb to which all test parameters have been referred.
2. During initial field evaluation and development of the Low-Drag Bomb, it was observed that on occasion the bomb would develop large pitching and yawing motions during the course of its trajectory. Subsequently it was conjectured that the cause of this somewhat erratic motion stemmed from the combined effects of the rolling motion, the pitch and yaw frequency, and the resulting yaw and Magnus moments which arise due to the roll and pitch characteristics of the bomb (reference a). In order to obtain experimental data that would help to explain such erratic missile motion as was observed, the Bureau of Ordnance directed the Naval Ordnance Laboratory to investigate the aerodynamic characteristics of the bomb.
3. As part of the subsequent Low-Drag Bomb program, NOL has conducted tests in recent months to determine the Magnus and static stability characteristics of the bomb at low-subsonic speeds ($V \leq 250$ feet per second), reference (b). More recently, NOL has tested the bomb in the Cornell Aeronautical Laboratory test facilities to determine the transonic aerodynamics of the configuration at angles of attack up to 22 degrees and Mach numbers from 0.60 to 1.25.
4. Using a 0.214-scale model of the bomb, six-component static data and Magnus force and moment characteristics were measured at spin rates scaled from the 1,000 pound bomb. The Magnus data were obtained at free-stream Reynolds numbers of 2×10^6 , 4×10^6 , and 6×10^6 , based on model total length. Static coefficients were obtained only at a free-stream Reynolds number of 4×10^6 . The figures showing static stability coefficients are presented in graphical form only for representative Mach numbers; however, a complete listing of the static coefficients for all test Mach numbers are tabulated in Appendix I.

Symbols

- A maximum body cross-sectional area (sq. ft.)
- C_A axial force coefficient
- C_N normal force coefficient = N/qA

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Symbols (Cont'd)

C_Y	side force coefficient = Y/qA
C_l	rolling moment coefficient = M_l / qAd
$C_{M_{c.g.}}$	pitching moment coefficient referred to the center of gravity = $M_{c.g.} / qAd$
$C_{\psi_{c.g.}}$	yawing moment coefficient referred to the center of gravity = $M_{\psi_{c.g.}} / qAd$
C_{Y_p}	Magnus force coefficient (side force coefficient due to spin) = $\frac{\partial Y}{\partial p} \cdot \frac{1}{qA} \cdot \frac{2V}{d}$
C_{ψ_p}	Magnus moment coefficient (yawing moment coefficient due to spin) = $\frac{\partial M_{\psi_{c.g.}}}{\partial p} \cdot \frac{1}{qA} \cdot \frac{2V}{d^2}$
C_{N_α}	slope of normal force coefficient through $\alpha = 0$ degrees
C_{m_α}	slope of pitching moment coefficient through $\alpha = 0$ degrees
d	maximum body diameter (ft.) = 1 (one) caliber
l	body length (ft.)
M_l	rolling moment (ft.-lbs.)
$M_{c.g.}$	pitching moment referred to the center of gravity (ft.-lbs.)
$M_{\psi_{c.g.}}$	yawing moment referred to the center of gravity (ft.-lbs.)
D	drag force (lbs.)
N	normal force (lbs.)
Y	side force (lbs.)
p	body rotational speed (radians/sec) - positive when model is rotating clockwise as viewed from the base
q	dynamic pressure (lbs./sq.ft.)
Re	Reynolds number = $\frac{\rho V l}{\mu}$
V	free-stream velocity (ft./sec.)
μ	absolute coefficient of viscosity of air (lbs.-sec./ft.sq.)
ρ	air density (slugs/cu.ft.)

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Symbols (Cont'd)

- α angle of attack (degrees)
- ψ angle of yaw (degrees)
- ϕ model roll angle - positive when model is rolled clockwise as viewed from the base

Test Apparatus and Procedure

5. The tests were conducted using the Cornell Aeronautical Laboratory 4 x 3 foot transonic cart. The cart is essentially a separate test section which can be placed in the normal 10 x 12 foot wind-tunnel test section. Speeds up to about Mach number 1.25 can be obtained. Normal angle of attack range is limited to approximately ± 15 degrees. However, for angles above 15 degrees, a "dog-leg" sting adapter may be used to extend the angle of attack range in one direction. Further information on the Cornell test facility may be found in reference (c).
6. The pertinent dimensions of the bomb configuration and the details of the mounting lugs are shown in Figure 2. In order to test at angles above 20 degrees, the model length was limited to approximately 24 inches and the maximum body diameter to 3 inches. Model spin was provided by a 7 H.P. 24,000 RPM, variable frequency, water-cooled motor mounted on the forward end of a strain-gaged balance beam. The motor was internally geared to the model by a 4.2:1 reduction gear. Strain-gage leads, motor wires, and water tubes were coupled to their respective power sources by running the leads through a hollow center core in the sting. Model spin was measured by a tachometer mounted in the rear of the motor section. From the tachometer signal, the spin rate was recorded in revolutions per minute on a Berkeley EPUT counter.
7. Magnus forces and moments acting on the model were measured by means of a four-component strain-gage balance designed and manufactured by the Naval Ordnance Laboratory. Since it was desirable to obtain the variation, if any, of the stability coefficients between a "minimum" spin rate (i.e., a spin rate just sufficient to "average" the normal forces and pitching moments due to static roll orientation--approximately 30 RPM) and the maximum test spin rate of 2,000 RPM, the balance was also designed to measure normal forces and pitching moments. Both the Magnus and "static" stability characteristics were obtained up to 22 degrees angle of attack in increments of four degrees. Test procedure for the Magnus measurements was to set the model at the desired angle of attack and slowly advance the model spin to the maximum rate. The output signals of the strain-gages measuring Magnus forces and moments were suitably amplified and supplied to the pen drive on a two-channel, Leeds and Northrup, Speed-O-Max recorder. By modifying the conventional time drive of the recorder chart to include a servo-motor

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driven by the model tachometer signal, it was possible to position the chart as a function of the model rotational speed and thus obtain a "trace" or record of the Magnus moment and pitching moment about each of the gage sections as a function of model spin rate for each angle of attack. However, due to the inability of the recorder chart to follow a tachometer signal corresponding to approximately 50 revolutions per minute or less, it was necessary to extrapolate the moment "traces" to zero rotational speed in order to obtain an initial slope through zero.

8. Six-component static measurements on the bomb were obtained using the CAL B-112 balance (reference d). Free-stream Reynolds number based on total model length was kept constant at 4×10^6 throughout the static measurements. Six-component data were obtained only to 22 degrees angle of attack for selected model roll positions from 0 degrees to 180 degrees.

Data Reduction

9. Within the experimental error, the Magnus moment "traces" obtained on the recorder charts were found to be linear with model rotational speed. It was sufficient, therefore, in determining coefficients, to use only the difference in the gage Magnus moment between the extrapolated zero RPM value and 2000 RPM. From this value, the Magnus coefficients, C_{Yp} and C_{Wp} , were converted to non-dimensional form by the relations

$$C_{Yp} = \frac{\partial Y}{\partial p} \cdot \frac{2V}{d} \cdot \frac{1}{qA}$$
$$C_{Wp} = \frac{\partial M_{x.c.g.}}{\partial p} \cdot \frac{2V}{d^2} \cdot \frac{1}{qA}$$

Normal force, pitching moment, side force, yawing moment, roll moment, and drag were reduced to the conventional coefficient forms as shown in the section under Symbols.

Precision of Data

10. The precision of the Magnus data obtained during the test is somewhat poorer than would be desirable. Since it was necessary that the Magnus balance measure relatively small forces and moments (Magnus forces in the order of 10 percent to 20 percent of the expected normal forces), as a consequence it was also sensitive to any random model oscillations or free-stream disturbances. From previous experience, it was expected that the recorder traces would show that the model was experiencing a somewhat erratic, high frequency small amplitude oscillation. Oscillations of this type are not surprising in view of the flexible balance used and the

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relatively high rotational speeds attained during the test. Past experience in similar tests has indicated that severe buffetting of the model will often occur at angles of attack above 10 to 15 degrees, depending on the spin rate and general configuration of the model. As a consequence, the "Magnus traces" consisted of "bands" whose limits were the maximum and minimum peaks of the high-frequency model oscillations. The value of the Magnus moment at any spin rate was then assumed to be the displacement of a point, on a mean line through the fluctuations, relative to any indicated moment due to static side forces which might arise at zero spin rate. Taking into account the model oscillations, plus the uncertainties involved in determining the test parameters, physical measurements and reader error, the probable error in the Magnus coefficients at various angles of attack has been estimated to have the following values:

α = angle of attack	C_{Yp}	C_{Yp}
4°	± 0.32	± 0.24
12°	± 0.45	± 0.49
22°	± 1.00	± 1.03

11. In view of the fairly large uncertainties in the Magnus data and plus the relatively small angle of attack correction indicated by a deflection load calibration, it was thought unnecessary to correct the Magnus data for pitch deflection loads at angle of attack. All the Magnus data shown in this report therefore are presented for indicated angles of attack only.

12. Uncertainties in the static data have been estimated from repeated measurements to be as follows:

C_N	$\pm .0046$
$C_{mc.g.}$	$\pm .0099$
C_Y	$\pm .0033$
$C_{yc.g.}$	$\pm .0045$
C_2	$\pm .0061$
C_A	$\pm .0035$

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Discussion of Results

13. With the advent in recent years of reliable dynamic test techniques, it has become of increasing value to include measurements of the Magnus forces and moments in wind-tunnel development tests of spinning, fin-stabilized configurations. Unstable flights of Weapon A and the 6-inch Test Vehicle (references e and f) together with subsequent calculations and dynamic wind-tunnel measurements, have borne out the necessity for Magnus measurements and their inclusion in the method of predicting the stability performance of any spinning, fin-stabilized configuration. Accordingly, developmental wind-tunnel tests of the Low-Drag Bomb have included measurements of the Magnus forces and moments acting on the bomb, at spin rates and angles of attack comparable to those which might be expected in free-flight tests.

14. Figures 3 through 11 present the Magnus force and moment coefficients of the bomb as a function of angle of attack for various Reynolds numbers and Mach numbers. The free-stream Reynolds number was held constant at 2×10^6 and 4×10^6 (based on total model length) for two separate Mach number runs from $M = 0.80$ to $M = 1.25$, and at 5×10^6 for a third Mach number run ranging only from $M = 0.60$ to $M = 0.95$.

15. Examination of Figures 3 through 10 shows that the variation of the Magnus coefficients is, in general, non-linear with increasing angle of attack. This is markedly so for the Magnus coefficients at free-stream Reynolds numbers of 2×10^6 . At this Reynolds number, the Magnus moment varies from negative values at $M = 1.25$ at all angles of attack, to positive values at a Mach number of $M = 1.00$ and below. The change in moment is due to oppositely directed Magnus forces rather than to movement of the center of pressure. At the higher free-stream Reynolds numbers of 4×10^6 and 6×10^6 the Magnus moment is positive throughout the respective range of test Mach numbers. An explanation for the "reversed" Magnus forces is not readily available. However, it has recently been observed by some experimenters (reference g) that at low subsonic speeds it is possible to generate either positive or negative Magnus forces, for example on a spinning cylinder in cross-flow, by varying the local Reynolds number around the periphery of the cylinder in such a way as to cause asymmetrical boundary-layer transition and/or separation. In this manner, the pressure distribution around the cylinder is such that the Magnus forces may act in either direction depending on the magnitude of the local Reynolds number and consequent boundary-layer separation position. It is conceivable then that the combination of the local cross-flow Reynolds number, model surface condition, and possible shock-boundary layer interaction along the model surface may set up conditions favorable to "reversed" Magnus forces such as those measured during the test. From Figures 3 through 10 it can be seen that the variation in the Magnus coefficients with Reynolds number is wide-spread. This is especially true for the higher

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angles of attack. In general, it is thought that much of the suspected Reynolds number effect believed to be present in the Magnus coefficients has been obliterated by the somewhat large experimental error in the "raw" Magnus data. The small magnitude of the Magnus forces and moments together with the relatively large normal forces and pitching moments experienced by the bomb impede, to a certain extent, compatible simultaneous measurements of these forces and moments using the type of balance system necessitated by the test parameters.

16. Figure 11 indicates that the Magnus force and moment characteristics of the bomb are highly non-linear with increasing Mach number, especially in the region of $M = 1.0$ and above. It is to be noted that Figure 11 shows the Magnus force and moment coefficient only at a spin rate of 2000 RPM and for a free-stream Reynolds number of 4×10^6 . However, since the Magnus data at any given angle of attack is linear with model spin rate, the data shown in Figure 11 are representative of the variation of the Magnus characteristics with Mach number for all spin rates, at least up to 2000 RPM. Note that the magnitude of the maximum Magnus moment (at $M = 0.60$) is only 15 percent of the maximum pitching moment of the bomb at 22 degrees angle of attack.

17. A previous investigation of the bomb at a Reynolds number of 6.3×10^6 and a Mach number of $M = 0.22$ (reference b) indicates that little change in the Magnus characteristics might be expected between $M = 0.60$ and $M = 0.22$.

18. Figures 12 through 19 show the normal force and pitching moment characteristics of the bomb for various roll orientations from 0 to 180 degrees. The zero degree roll position is taken to be the position of the model when the mounting lugs (Figure 2) lie in the pitch plane of the model and the fins are displaced 45 degrees from that plane. Figures 12 through 19 also show the variation of the normal force center of pressure with angle of attack for various roll positions. It is evident from examination of these data that the bomb is statically stable throughout the test Mach number range. To be noted is the expected large variation in pitching moment and normal force that occurs as the model is rolled 45 degrees from the zero roll position. In general, at 22 degrees angle of attack an average increase of 75 percent in the pitching moment coefficient occurs for a roll displacement of 45 degrees from the zero roll position at Mach numbers of $M = 0.60$ through $M = 1.25$. Similar increases in the normal force coefficients amount to approximately 10 percent at $M = 1.25$ to about 25 percent at $M = 0.60$. The center of pressure travel due to angle of attack increase is relatively small, varying less than one-half caliber at most Mach numbers.

19. Figure 20 indicates that the variation of the normal-force and pitching-moment coefficients with Mach number is generally slight for Mach numbers below approximately $M = 1.0$. An appreciable variation is noted, however, at

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angles of attack above 16 degrees where a somewhat precipitate drop in the pitching-moment coefficient occurs as the Mach number is increased beyond $M = 1.0$. The decrease is due, however, to a forward travel in the center of pressure rather than a loss in lift.

20. Figure 21 shows a comparison of the normal-force and pitching-moment coefficient slopes, C_{N_L} and C_{m_L} , respectively, from wind-tunnel and free-flight measurements (reference g). The cross-hatched band depicts the maximum and minimum limits of the slopes due to static model roll positions of $\phi = 45^\circ$ and $\phi = 0^\circ$ respectively. As indicated on the plot, the broken curves illustrate the variation of the slopes as determined from free-flight measurements in the NOL Pressurized Ballistics Range and from wind-tunnel measurements made with the model spinning at the maximum rate of 2000 RPM. Data from these tests are considered to be somewhat less reliable than the static or free-flight data since considerable scatter was present in the coefficients at low angles of attack. These latter measurements were, of course, subject to the same disturbances as previously cited for the Magnus measurements and because of this are plotted only for a qualitative comparison with the static and free-flight slopes. As can be noted from Figure 21, the normal-force coefficient slopes from the static and free-flight data agree quite well except at the higher Mach numbers above approximately $M = 1.05$. The moment slopes are not in as good agreement, the free-flight data indicating less "stability" at Mach numbers in the range $0.9 \leq M \leq 1.1$ and somewhat higher "stability" in the immediate range around $M = 1.0$ than is indicated by the wind-tunnel data.

21. In reference to Figures 22 through 25, it is usually assumed that a cruciform finned projectile pitched at an arbitrary angle of attack will experience no side force or yawing moment as long as the fins are in a symmetrical position relative to the pitch plane. If the projectile is rolled about the longitudinal axis until the fins are no longer symmetrical relative to the pitch plane, a side force and yawing moment will appear which are dependent on the roll angle ϕ , and the magnitude of the angle of attack, α . Reference (a), in discussing the action of the yawing moment in connection with the phenomenon of so-called "catastrophic yaw," suggests that for certain special cases the yawing moment may combine with the Magnus moment and thus give rise to the occasionally-observed large pitching and yawing motions of spinning, fin-stabilized missiles.

22. Figures 22 through 25 show the variation of the side force and yawing moment coefficients with model roll angle for various angles of attack. As is evident from these data, the coefficients are roughly proportional to $\sin 4\phi$ at any arbitrary angle of attack. It is to be noted that the indicated test points on these plots have been adjusted by an amount equal to the displacement of the side force or yawing moment coefficient from the zero coefficient value at zero angle of attack for each roll position. The "uncorrected" values of the side force and yawing moment coefficients are tabulated in the Appendix. The small "trim" angles in the data at zero angle of attack were assumed to arise from misalignments of the model along the tunnel centerline and not from aerodynamic causes.

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23. As previously mentioned, reference (a) suggests that for certain cases (viz., "lunar motion" or "resonance") the yawing and Magnus moments acting on a finned missile may combine when the missile is rolled at an angle such that the moments are of the same sign. It may be seen from Figures 22 through 25 that these "critical" angle ranges for the bomb apparently occur in the vicinity of $55^\circ \leq \phi \leq 85^\circ$, and $135^\circ \leq \phi \leq 180^\circ$. Note that the magnitude of the yawing moment is considerably less for $55^\circ \leq \phi \leq 85^\circ$. In this range, the mounting lugs are located in the lee-side of the model and skewed relative to the pitch plane at angles of attack. Thus, it is possible that the lugs may influence the body-shed vortices in such a manner as to introduce an interference effect which would be felt by the fins with a resultant variation in the magnitude of the yawing moment in this roll angle range.

24. In general, the yawing moment is little affected by Mach number at angles of attack of 16 degrees and below. At higher angles, however, and, in particular at model roll angles where the peak, positive yawing moments occur, the variation of the yaw moment with Mach number is somewhat erratic and inconclusive.

25. Static rolling moment coefficients are shown in Figures 26 through 29 as a function of model angle of attack and roll orientation. As may be noted from these plots, the rolling moment coefficient is also roughly dependent on $\sin \phi$, at least for angles of attack of 16 degrees and above. The relatively constant moment experienced by the model at angles of attack of 12 degrees and below indicate that little or no induced roll effects are present at these angles.

26. The variation of the roll moment coefficient with Mach number appears to be negligible at 12 degrees angle of attack and below. At the higher angles, however, if the peak positive and negative moments are considered, the maximum moments show somewhat different characteristics. In general, it is seen that for roll angles of ϕ equal to approximately 22.5 and 112.5 degrees, the tendency of the maximum roll coefficient is to decrease with increasing Mach number from $M = 0.60$ to $M = 1.25$. For roll angles of $\phi = 67.5$ degrees and 157.5 degrees, the roll coefficient generally increases (i.e., a larger negative moment in this case) except for a small region between $M = 0.90$ to $M = 1.0$. Here, the rolling moment coefficient decreases quite rapidly, appearing almost as a discontinuity for certain angles of attack, but increasing once again beyond $M = 1.0$.

27. Figure 30 shows the variation of the spin parameter, $pd/2V$, as a function of angle of attack for various Mach numbers. For these tests, it was desired to obtain some idea of the equilibrium spin rate of the bomb with increasing angle of attack. By removing the motor and gearing structure the model was free to rotate, presumably somewhere near the equilibrium spin rate. Since it was not possible to determine the bearing friction in the model, Figure 30 shows only a qualitative representation of the spin history. From these data it appears that the model spin reaches a

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maximum at some angle of attack around 18 - 20 degrees for the lower Mach numbers. Above $M = 0.95$, however, a peak is reached at somewhat lower angles. Note the fairly rapid drop in spin rate that occurs around $M = 1.25$.

28. Previous low-speed investigations on the Low-Drag Bomb (NOL unpublished data) have indicated that a similar "speed-up" in roll rate occurs when the bomb is subjected to angles of attack above approximately 30 degrees. Results of these tests show that the spin rate can approach values as high as four times the zero angle of attack roll rate, depending on the angle of attack. Tests are presently being carried out in the Smoke Tunnel at the University of Notre Dame in an effort to determine and subsequently control the aerodynamic mechanism governing the roll speed-up phenomenon.

29. Figure 31 presents the zero-lift drag coefficient of the bomb with and without mounting lugs attached to the bomb. For comparison, the total zero-lift drag coefficient of the bomb determined from firings of a 0.056-scale model with lugs in the NOL Pressurized Ballistics Range is also shown (reference g). It should be noted that the wind-tunnel coefficients have been adjusted to zero base drag. Accordingly, the solid curves in Figure 31 are representative of only the wave drag plus skin friction drag of the model. It may be noted from these curves that the drag coefficient shows the characteristic transonic drag rise at approximately $M = 1.05$ to 1.10. The increase in drag due to mounting lugs is fairly consistent throughout the Mach number range, averaging approximately 0.025 in terms of the coefficient value.

Summary

30. In summary, the results presented in this report show that the Magnus force and moment coefficients of the bomb are linearly dependent on the bomb rotational speed. It is seen that the Magnus force and moment are also dependent on the free-stream Reynolds number in some cases being of opposite sign due to reversed Magnus forces experienced at the lower Reynolds numbers. In addition, the Magnus coefficients are seen to be generally non-linear with angle of attack and of relatively small magnitude compared to the static normal force and pitching moment coefficients.

31. The results also show the bomb to be statically stable at all angles of attack. It is seen that static normal forces and pitching moments vary appreciably with fin-roll orientation. A roll displacement of 45 degrees from the zero roll position can increase the pitching moment by approximately 75 percent and the normal force up to 25 percent. Static side forces and moments, and static rolling moments, were also found to be non-linear with increasing angle of attack. Variation of these coefficients with model roll angle is roughly proportional to $\sin 4\phi$ for angles of attack above approximately 12 degrees. In addition, it is seen that the drag rise due

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to mounting lugs is fairly small over the test Mach number range, averaging only 0.025 in terms of the coefficient value.

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TABLE I
Test Conditions

Run	Mach No.	Dynamic Pressure (lbs/ft ²) \pm 1 psf	Reynolds No. (Re x 10 ⁻⁶)	Measure- ment	Roll Angle (ϕ -Degrees)
1	1.25	213	2	Magnus	
2	1.20	205	2	Magnus	
3	1.10	197	2	Magnus	
4	1.00	187	2	Magnus	
5	0.95	180	2	Magnus	
6	0.90	177	2	Magnus	
7	0.80	162	2	Magnus	
8	1.25	427	4	Magnus	
9	1.00	374	4	Magnus	
10	1.20	411	4	Magnus	
11	1.10	394	4	Magnus	
12	0.95	359	4	Magnus	
13	0.90	348	4	Magnus	
14	0.80	317	4	Magnus	
15	0.95	539	6	Magnus	
16	0.90	514	6	Magnus	
17	0.80	477	6	Magnus	
18	0.60	384	6	Magnus	
19	0.60	384	6	Magnus	
47	1.25	427	4	6-compo- nent static	0°
48	1.20	411	4	6-compo- nent static	0°
49	1.10	394	4	6-compo- nent static	0°
50	1.00	374	4	6-compo- nent static	0°
51	0.95	359	4	6-compo- nent static	0°
52	0.90	348	2	6-compo- nent static	0°
53	0.80	317	4	6-compo- nent static	0°

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TABLE I (Cont'd)

Run	Mach No.	Dynamic Pressure (lbs/ft ²) \pm 1 psf	Reynolds No. (Re x 10 ⁻⁶)	Measure- ment	Roll Angle (β -Degrees)
54	0.60	251	4	6-compo- nent static	0°
55	1.25	427	4	6-compo- nent static	11.25°
56	1.00	374	4	6-compo- nent static	11.25°
57	0.90	348	4	6-compo- nent static	11.25°
58	0.60	251	4	6-compo- nent static	11.25°
59	1.25	427	4	6-compo- nent static	22.50°
60	1.10	394	4	6-compo- nent static	22.50°
61	1.00	374	4	6-compo- nent static	22.50°
62	0.90	348	4	6-compo- nent static	22.50°
63	0.60	251	4	6-compo- nent static	22.50°
64	1.25	427	4	6-compo- nent static	33.75°
65	1.00	374	4	6-compo- nent static	33.75°
66	0.90	348	4	6-compo- nent static	33.75°
67	0.60	251	4	6-compo- nent static	33.75°
68	1.25	427	4	6-compo- nent static	45.00°

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TABLE I (Cont'd)

Run	Mach No.	Dynamic Pressure (lbs/ft ²) \pm 1 psf	Reynolds No. (Re x 10 ⁻⁶)	Measure- ment	Roll Angle (ϕ Degrees)
69	1.10	394	4	6-compo- nent static	45.00°
70	1.00	374	4	6-compo- nent static	45.00°
71	0.90	348	4	6-compo- nent static	45.00°
72	0.60	251	4	6-compo- nent static	45.00°
73	1.25	427	4	6-compo- nent static	67.50°
74	1.00	374	4	6-compo- nent static	67.50°
75	0.90	348	4	6-compo- nent static	67.50°
76	0.60	251	4	6-compo- nent static	67.50°
77	1.25	427	4	6-compo- nent static	90.00°
78	1.00	374	4	6-compo- nent static	90.00°
79	0.90	348	4	6-compo- nent static	90.00°
80	0.60	251	4	6-compo- nent static	90.00°
81	1.25	427	4	6-compo- nent static	112.50°
82	1.00	374	4	6-compo- nent static	112.50°
83	0.90	348	4	6-compo- nent static	112.50°

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TABLE I (Cont'd)

Run	Mach No.	Dynamic Pressure (lbs/ft ²) + 1 psf	Reynolds No. (Re x 10 ⁻⁶)	Measure- ment	Roll Angle (ϕ -Degrees)
84	0.60	251	4	6-compo- nent static	112.50°
85	1.25	427	4	6-compo- nent static	135.00°
86	1.00	374	4	6-compo- nent static	135.00°
87	0.90	348	4	6-compo- nent static	135.00°
88	0.60	251	4	6-compo- nent static	135.00°
89	1.25	427	4	6-compo- nent static	157.00°
90	1.00	374	4	6-compo- nent static	157.00°
91	0.90	348	4	6-compo- nent static	157.00°
92	0.60	251	4	6-compo- nent static	157.00°
93	1.25	427	4	6-compo- nent static	180.00°
94	1.20	411	4	6-compo- nent static	180.00°
95	1.10	394	4	6-compo- nent static	180.00°
96	1.00	374	4	6-compo- nent static	180.00°
97	0.90	348	4	6-compo- nent static	180.00°
98	0.60	251	4	6-compo- nent static	180.00°

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Appendix

The Appendix lists the static coefficients obtained at a Reynolds number of 4×10^6 for various roll angles from 0 degrees to 180 degrees. Column nomenclature is listed at the top of the columns as shown on the first page of the tabulated data.

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Run	Point No.	Mach No.	α	ϕ	ψ	CH	CM _{C.G.}	CY	C _{C.G.}	C _A	C _A
47	02	1.25	8.14	.00	.00	.60354	1.81387-	.02734-	.07574	.04369	.27456
47	03	1.25	12.25	.00	.00	1.07834	1.19477-	.04037-	.03026	.04472	.28425
47	04	1.25	16.39	.00	.01	1.52250	1.59950-	.04579-	.00094	.03465	.29170
47	05	1.25	20.68	.00	.00	2.32987	1.59963-	.06009-	.15029	.00331-	.29278
47	07	1.25	.00	.00	.00	.02056	.02085-	.01929-	.06090	.01743	.25136
48	02	1.20	.01	.00	.01	.03397	1.0555-	.00742	.07030-	.02342	.24904
48	03	1.20	3.11	.00	.02	.72659	1.07658-	.00034-	.07701-	.03737	.26879
48	04	1.20	12.23	.00	.02	1.13796	1.54206-	.00233-	.09486-	.03896	.28107
48	05	1.20	15.34	.00	.03	1.58612	1.79824-	.00206-	.10314-	.02858	.28617
48	06	1.20	20.60	.00	.02	2.26000	1.92074-	.00446-	.05873-	.00563	.28071
48	07	1.20	22.77	.00	.01	2.75101	2.00915-	.10395-	.25956	.01363	.28133
48	08	1.20	.00	.00	.01	.03259	1.0414-	.01478	.07309-	.01828	.25259
49	02	1.10	.01	.00	.00	.00429-	.09970	.00209	.01170	.03090	.24802
49	03	1.10	8.12	.00	.00	.62339	.60739-	.01058	.02828-	.03864	.25259
49	04	1.10	12.24	.00	.00	1.05648	1.18273-	.00732	.02651-	.04017	.26049
49	06	1.10	16.35	.00	.01	1.48099	1.47355-	.00206	.06737-	.03809	.26387
49	07	1.10	20.51	.00	.02	1.98009	1.49025-	.01811	.12007-	.01689	.27750
49	08	1.10	22.69	.00	.02	2.47003	1.65413-	.05263	.20240-	.00152-	.27876
49	09	1.10	.01	.00	.00	.00469-	.09357	.00395	.01271	.01977	.24942
50	01	1.00	.00	.00	.00	.00423	.00368-	.00235	.00378	.01654	.11712
50	02	1.00	8.10	.00	.00	.56539	.70969-	.00219-	.00913-	.02347	.11781
50	03	1.00	12.18	.00	.01	.99120	1.27680-	.00048	.03493-	.02796	.12152
50	04	1.00	16.27	.00	.00	1.42301	1.77137-	.00760-	.00616-	.01388	.10484
50	05	1.00	20.39	.00	.01	1.95471	2.19375-	.00489-	.01980-	.00960	.09057
50	06	1.00	22.49	.00	.02	2.20121	2.13564-	.00368	.11055-	.00016	.07943
50	07	1.00	.01	.00	.03	.00471-	.00802	.00233	.00643	.01243	.11724

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51	02	0.95	01-	00	00	00755-	02263	00809-	01452	03540	09181
51	03	0.95	8.09	00	01-	57249	70417-	01245-	00028	04982	09283
51	04	0.95	12.16	00	01-	94572	1.24442-	02005-	01165	04497	09092
51	05	0.95	16.23	00	00	1.36297	1.72336-	02808-	05467	04217	08380
51	06	0.95	20.35	00	02-	1.82334	2.04945-	00049-	09917-	01488	06543
51	07	0.95	22.44	00	03-	2.05614	2.09627-	02859	22921-	01512	05949
51	08	0.95	00	00	00	01225-	02594	00589-	01283	03532	09300
52	01	0.90	01-	00	00	00806-	01748	00620-	01241	03330	08783
52	02	0.90	0.09	00	01-	55597	59879-	01063-	00362-	04527	08789
52	03	0.90	12.14	00	01-	92016	1.24320-	01828-	01029	04341	08788
52	04	0.90	16.22	00	00	1.34256	1.72016-	03122-	04755	04057	08036
52	05	0.90	20.32	00	02-	1.75937	2.00935-	00385-	07811-	02170	06511
52	06	0.90	22.39	00	03-	1.97465	2.05553-	00919	15033-	01235	05897
52	08	0.90	00	00	00	00835-	01792	00402-	00894	03015	08857
53	02	0.80	01-	00	00	01444-	03001	00443-	00975	02864	08441
53	03	0.80	8.07	00	03	55107	70024-	00653-	00765-	04170	08518
53	04	0.80	12.14	00	01-	91644	1.22972-	00762-	01628-	04330	08676
53	05	0.80	15.18	00	00	1.29538	1.70136-	03265-	04777	07435	07703
53	06	0.80	20.27	00	01-	1.69471	2.00830-	01922-	00028	02324	06602
53	07	0.80	22.34	00	01-	1.88117	2.07935-	01380-	04078-	02345	06343
54	02	0.60	01-	00	00	01173-	03341	00884-	01474	03056	07940
54	03	0.60	9.06	00	00	53778	69309-	02912-	05729	04725	08189
54	04	0.60	12.09	00	00	88546	1.22072-	02095-	01527	04479	08092
54	05	0.60	16.13	00	00	1.26595	1.75410-	02222-	01971	03714	07206
54	06	0.60	20.18	00	01-	1.63035	2.12582-	01829-	00328-	02079	06659
54	07	0.60	22.23	00	01-	1.03477	2.29046-	01652-	00895-	02108	06257
54	08	0.60	00	00	00	01070-	02418	01165-	00094	03484	07781

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108 02	1.20	.00	22.50	.01-	.04484	.11801-	.01880	.09198-	.02929	.21077
108 03	1.20	8.12	22.50	.03-	.72166	1.17986-	.04988	.24910-	.03663	.23577
108 04	1.20	12.20	22.50	.07-	1.18251	1.72041-	.11045	.56740-	.04274	.25367
108 05	1.20	16.33	22.50	.10-	1.64234	2.01881-	.18322	.85874-	.06811	.26429
108 06	1.20	20.39	22.50	.13-	2.40239	2.35281-	.23068	.09123-	.09568	.26742
108 07	1.20	23.13	22.50	.11-	4.17021	3.36710-	.12902	.77099-	.10394	.26400
108 08	1.20	.00	22.50	.01-	.05300	.12377-	.01485	.08876-	.02420	.21576
109 09	1.10	.00	22.50	.00	.333	.07861	.00978	.00435-	.02554	.21942
109 10	1.10	8.12	22.50	.01-	.66683	.80364-	.04938	.17547-	.02680	.22685
109 11	1.10	12.21	22.50	.05-	1.09016	1.37641-	.12579	.52697-	.02434	.23267
109 12	1.10	16.32	22.50	.10-	1.55155	1.75118-	.21251	.94352-	.04670	.24392
109 13	1.10	20.52	22.50	.13-	2.09549	1.88745-	.26749	.17492-	.06991	.25756
109 14	1.10	22.68	22.50	.13-	2.64949	2.22785-	.27654	.22616-	.06943	.25777
109 15	1.10	.00	22.50	.00	.00332	.07855	.00974	.00431-	.02076	.21973
110 02	0.60	.01-	22.50	.00	.00349-	.01062	.01492-	.01924	.03803	.05662
110 03	0.60	8.04	22.50	.01-	.55229	.77324-	.01638	.12905-	.05134	.06131
110 04	0.60	12.08	22.50	.03-	.92455	1.40046-	.07888	.38274-	.04595	.06371
110 05	0.60	16.11	22.50	.06-	1.33513	2.04471-	.17418	.81322-	.06265	.06001
110 06	0.60	20.16	22.50	.08-	1.73938	2.49460-	.24176	.12493-	.11320	.05492
110 07	0.60	.22	22.50	.09-	1.93083	2.68695-	.26176	.21315-	.13152	.05209
110 08	0.60	.01-	22.50	.00	.01152-	.02551	.00561-	.00828	.04216	.05534

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55	02	1.25	.00	11.25	.00	.01260	.00012-	.01935-	.00354	.02466	.24736
55	03	1.25	5.15	11.25	.00	.69434	.83715-	.00824	.02443-	.02614	.27657
55	04	1.25	12.25	11.25	.02-	1.11186	1.26066-	.06440	.23846-	.02037	.28682
55	05	1.25	16.39	11.25	.05-	1.56535	1.46989-	.08299	.40047-	.03677	.29360
55	06	1.25	22.17	11.25	.03-	2.12255	1.85341-	.15432	.66792-	.04326	.30042
55	07	1.25	25.66	11.25	.07-	2.32355	1.69555-	.16246	.66269-	.02630	.30311
55	08	1.25	.00	11.25	.00	.02036	.02073-	.01917-	.06046	.01499	.25336
55	09	1.25	.00	11.25	.00	.00862-	.02300	.00044	.00221	.03226	.10284
55	10	1.00	.00	11.25	.00	.55765	.67783-	.03455	.09223-	.02610	.10803
55	11	1.00	8.10	11.25	.00	.97520	1.27955-	.08947	.30932-	.01935	.10794
55	12	1.00	12.17	11.25	.02-	1.44119	1.84551-	.13770	.53621-	.03838	.10440
55	13	1.00	16.26	11.25	.05-	1.51014	2.21276-	.15561	.52342-	.06452	.10228
55	14	1.00	20.38	11.25	.04-	2.29501	2.25581-	.16121	.52303-	.08697	.09693
55	15	1.00	22.49	11.25	.03-	.57526	.66653-	.04030	.10566-	.02039	.11653
55	16	1.00	5.10	11.25	.00	.01707-	.03455	.00034	.09271	.02568	.11455
55	17	1.00	.01-	11.25	.00	.56908	.73198-	.03550	.10015-	.02377	.09539
55	18	0.90	8.08	11.25	.00	.94582	1.29871-	.07995	.27407-	.01626	.09356
55	19	0.90	12.14	11.25	.02-	1.36859	1.63124-	.14985	.55695-	.01611	.08913
55	20	0.90	16.21	11.25	.04-	1.78590	2.10256-	.13982	.43890-	.06212	.08678
55	21	0.90	20.32	11.25	.02-	2.01422	2.22655-	.14539	.44395-	.07129	.08189
55	22	0.90	24.39	11.25	.02-	.00511-	.00960	.00476	.00051-	.02114	.09621
55	23	0.90	.01	11.25	.00	.02544-	.05245	.00256-	.00610	.03912	.07812
55	24	0.60	.01-	11.25	.00	.53925	.70133-	.02276	.05352-	.04753	.08068
55	25	0.60	8.05	11.25	.00	.89326	1.28255-	.06369	.24275-	.03700	.08164
55	26	0.60	12.09	11.25	.01-	1.26150	1.53195-	.11692	.48566-	.04371	.07292
55	27	0.60	16.13	11.25	.03-	1.64596	2.22757-	.18623	.75093-	.06774	.06824
55	28	0.60	20.16	11.25	.05-	1.83404	2.35013-	.21168	.79655-	.07701	.06803
55	29	0.60	22.22	11.25	.04-	.04381-	.05091	.01169-	.01609	.04768	.07937
55	30	0.60	.01-	11.25	.00	.00	.00	.00	.00	.00	.00

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57	02	1.25	.00	22.50	.00	.01869	.02047-	.03023-	.07634	.02752	.24872
58	03	1.25	8.14	22.50	.00	.70085	.86843-	.05108	.12743-	.01601	.27474
59	04	1.25	12.24	22.50	.04-	1.12465	1.39911-	.11597	.43048-	.02142	.28525
60	05	1.25	16.37	22.50	.09-	1.56920	1.64605-	.16849	.74504-	.04371	.29183
61	06	1.25	20.66	22.50	.12-	2.39952	2.02273-	.16047	.91605-	.07211	.30079
62	07	1.25	22.82	22.50	.12-	2.92761	2.22629-	.14422	.81908-	.08348	.30075
63	08	1.25	.01	22.50	.00	.01521	.01616-	.02096-	.06653	.01504	.25448
64	09	1.10	.00	22.50	.01	.01292-	.10021	.00613	.01111	.03051	.24302
65	00	1.10	5.13	22.50	.00	.65039	.72423-	.09633	.18704-	.01697	.25735
66	01	1.10	12.20	22.50	.04-	1.09159	1.30540-	.16525	.53572-	.00290	.25520
67	02	1.10	16.31	22.50	.09-	1.53394	1.01663-	.26932	.00937-	.02280	.26489
68	03	1.10	20.49	22.50	.11-	2.04934	1.90504-	.26440	.10753-	.06519	.27542
69	04	1.10	22.65	22.50	.12-	2.53712	2.08678-	.26016	.12482-	.07354	.28876
70	05	1.10	.50	22.50	.00	.00349-	.05609	.01131	.00804-	.02026	.25627
71	06	1.00	.00	22.50	.00	.00916-	.01765	.00442	.00035-	.01837	.11593
72	07	1.00	8.10	22.50	.00	.58922	.75823-	.06741	.16855-	.00921	.11833
73	08	1.00	12.17	22.50	.03-	1.02276	1.47003-	.14531	.47264-	.00696	.11865
74	09	1.00	16.24	22.50	.06-	1.48050	2.09593-	.22632	.97076-	.03505	.11032
75	00	1.00	20.37	22.50	.08-	1.95655	2.45719-	.21285	.85645-	.09383	.10409
76	01	1.00	22.48	22.50	.02-	2.28386	2.53883-	.24065	.93530-	.11663	.10190
77	02	1.00	.01-	22.50	.00	.00091-	.00047	.00047	.00604-	.01251	.11826

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61 01	1.90	8.99	22.50	.00	.59238	.81740-	.06880	.17852-	.00866	.10249
61 02	0.90	14.13	22.50	.01-	.88130	1.46671-	.14377	.47683-	.00194	.10149
62 03	0.90	16.20	22.50	.07-	1.39322	1.99279-	.41873	.85580-	.03638	.09724
62 04	0.90	20.30	22.50	.07-	1.32145	2.31670-	.19909	.80210-	.09959	.09033
62 05	0.90	22.37	22.50	.08-	2.04911	2.50680-	.17967	.79319-	.11894	.08298
63 02	0.60	.01-	22.50	.00	.00515-	.01279	.00259-	.00219	.03950	.07972
63 03	0.60	5.05	22.50	.01-	.56247	.78129-	.03787	.14946-	.03934	.08117
63 04	0.60	12.08	22.50	.02-	.92544	1.40934-	.10658	.40341-	.03376	.08338
63 05	0.60	16.15	22.50	.05-	1.33682	2.07661-	.22931	.83498-	.05015	.07476
63 06	0.60	20.18	22.50	.08-	1.72246	2.52152-	.28181	.18584-	.10116	.07202
63 07	0.60	22.21	22.50	.08-	1.90897	2.71211-	.28031	.22981-	.13238	.06778
63 08	0.60	.00	22.50	.00	.00925-	.02373	.01798-	.01776	.04961	.07826

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54	02	1.25	01-	33.75	.00	.01353	.00096-	.02501-	.07102	.02474	.24505
54	03	1.25	014	33.75	.00	.72305	.00025-	.04291	.09555-	.01875	.27442
54	04	1.25	12.14	33.75	.04-	1.15085	1.26395-	.13116	.40554-	.01418	.28693
54	05	1.25	16.56	33.75	.10-	1.65260	1.89712-	.22496	.91166-	.03213	.29442
54	06	1.25	20.64	33.75	.13-	2.45357	2.45773-	.24770	.10400-	.06053	.30013
54	07	1.25	22.65	33.75	.12-	3.03750	3.07725-	.12267	.80413-	.07622	.29254
54	08	1.25	.00	33.75	.01	.01653	.00907-	.02268-	.07271	.01475	.25049
55	01	1.00	01-	33.75	.00	.01370-	.02723	.00661	.00465-	.02938	.10834
55	02	1.00	009	33.75	.00	.62249	.02577-	.05925	.15684-	.01802	.11537
55	03	1.00	11.17	33.75	.03-	1.07043	1.05501-	.13910	.47204-	.01228	.11727
55	04	1.00	16.25	33.75	.07-	1.60114	2.021490-	.25222	.91675-	.03545	.10697
55	05	1.00	20.35	33.75	.09-	2.09385	3.02087-	.27203	.05939-	.08266	.08916
55	06	1.00	22.44	33.75	.10-	2.30897	3.22215-	.20716	.93964-	.10514	.07420
55	07	1.00	.01-	33.75	.00	.01215-	.02616	.00230	.00117	.02974	.11170
56	01	0.90	01-	33.75	.00	.00947-	.01914	.00247	.00156-	.01772	.09178
56	02	0.90	008	33.75	.01-	.01397	.30513-	.05503	.15513-	.00367	.09841
56	03	0.90	12.13	33.75	.02-	1.04205	1.66574-	.15091	.49216-	.00545	.09982
56	04	0.90	16.20	33.75	.07-	1.43024	2.28298-	.28151	.00489-	.04008	.09761
56	05	0.90	20.29	33.75	.09-	1.92354	2.75393-	.28371	.07684-	.09138	.08753
56	06	0.90	22.35	33.75	.07-	2.16165	2.95512-	.22792	.97479-	.12248	.07411
57	01	0.80	01-	33.75	.00	.01134-	.02541	.00505-	.00842	.03242	.07991
57	02	0.80	005	33.75	.01-	.56102	.34092-	.04415	.15399-	.03955	.08411
57	03	0.80	12.09	33.75	.02-	.93406	1.60133-	.12437	.44718-	.03425	.08814
57	04	0.80	16.11	33.75	.03-	1.40229	2.06453-	.26862	.95952-	.04266	.08494
57	05	0.80	20.16	33.75	.07-	1.82049	2.93613-	.38935	.48435-	.09430	.07864
57	06	0.80	22.10	33.75	.09-	2.04174	3.19404-	.41916	.59433-	.11709	.07435
57	07	0.80	.01-	33.75	.00	.00414-	.01173	.00664-	.01064	.04795	.07716

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68 01	1.00	.00	45.00	.01	.01655	.00377-	.02116-	.07190	.02474	.24530
68 02	1.25	.14	45.00	.01	.74384	1.04044-	.03611	.02723-	.01650	.27778
68 03	1.25	12.24	45.00	.01-	1.00751	1.05010-	.07685	.20931-	.01616	.29294
68 04	1.10	16.56	45.00	.04-	1.71037	1.11901-	.24300	.65177-	.00525	.29625
68 05	1.25	20.82	45.00	.06-	2.02074	2.02771-	.15140	.09546-	.00454	.29450
68 06	1.25	22.83	45.00	.07-	2.07742	2.08215-	.15113	.00557-	.01906	.28438
68 07	1.25	.00	45.00	.01	.02775	.02214-	.02495-	.07271	.01468	.24570
69 02	1.10	.00	45.00	.01	.00559-	.10054	.00797	.00972	.02509	.24516
69 03	1.10	8.15	45.00	.01	.70771	.09905-	.02062	.05542-	.01672	.25623
69 04	1.10	12.21	45.00	.01	1.19356	1.71457-	.11560	.25025-	.01100	.26587
69 05	1.10	16.30	45.00	.02-	1.69543	2.04311-	.23277	.60203-	.00486	.27115
69 06	1.10	20.47	45.00	.07-	2.17566	2.70300-	.34953	.06556-	.02187	.28921
69 07	1.10	22.62	45.00	.05-	2.70797	3.01477-	.22651	.74026-	.05565	.29227
69 08	1.10	.00	45.00	.01	.01001-	.10324	.00582	.01075	.01662	.24960
70 01	1.00	.01-	45.00	.00	.01415-	.05330	.00640	.00705-	.01507	.11332
70 02	1.00	8.10	45.00	.01	.65622	.85511-	.04966	.06418-	.00697	.11852
70 03	1.00	12.15	45.00	.00	1.12046	1.79740-	.10358	.22891-	.00316-	.12289
70 04	1.00	16.22	45.00	.01-	1.65254	2.75955-	.21523	.55801-	.00970-	.11390
70 05	1.00	20.33	45.00	.04-	2.21431	3.05860-	.30053	.06955-	.01170	.09093
70 06	1.00	22.42	45.00	.05-	2.54717	3.72204-	.26363	.84738-	.02224	.06981
70 07	1.00	.01-	45.00	.00	.00000-	.01493	.00423	.00540-	.00520	.11811

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71 02 0.90	.01-	45.00	.00	.00125	.00036-	.00136-	.00114-	.03036	.08921
71 04 0.90	8.09	45.00	.00	.64096	.90021-	.02955	.05641-	.04083	.09535
71 05 0.90	12.13	45.00	.00	1.10093	1.80533-	.10610	.23771-	.01071	.09899
71 06 0.90	16.19	45.00	.00	1.61593	2.79933-	.24213	.69175-	.01384	.09425
71 07 0.90	20.23	45.00	.00	2.11670	3.41397-	.36513	.13419-	.05669	.08142
71 08 0.90	24.34	45.00	.07	2.39322	3.01510-	.34833	.13545-	.08151	.06633
71 09 0.90	.00	45.00	.00	.00095	.00534	.00193-	.00104-	.02406	.09109
72 02 0.60	.00	45.00	.00	.00442-	.02060	.00877-	.00667	.04374	.07739
72 03 0.60	8.09	45.00	.00	.61503	.91327-	.02318	.06054-	.05932	.08474
72 04 0.60	12.08	45.00	.00	1.02404	1.72221-	.03077	.21711-	.03375	.09145
72 05 0.60	16.11	45.00	.02	1.51158	2.60539-	.21049	.62145-	.03254	.08418
72 06 0.60	20.16	45.00	.00	2.01110	3.50734-	.41243	.36112-	.05466	.07789
72 07 0.60	24.23	45.00	.07	2.25186	3.90204-	.46131	.22426-	.06508	.07176
72 08 0.60	.01-	45.00	.00	.00401	.00627	.01803-	.01305	.04816	.07719

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72 01	1.25	.00	67.50	.01	.01890	.00000-	.01000-	.06787	.01976	.24833
73 02	1.25	.010	67.50	.02	.71971	.00000-	.01000-	.25530	.02012	.27944
73 03	1.25	.020	67.50	.03	1.10040	.00000-	.01000-	.37659	.01029-	.29030
73 04	1.25	.030	67.50	.04	1.71244	.00000-	.01000-	.29761	.05927-	.29260
73 05	1.25	.040	67.50	.05	2.40345	.00000-	.01000-	.17978	.08619-	.29355
73 06	1.25	.050	67.50	.06	1.90090	.00000-	.01000-	.43209	.07402-	.29035
73 07	1.25	.060	67.50	.07	.00073	.00000-	.01000-	.00000	.00000	.25552
74 01	1.00	.01-	67.50	.00	.00004	.00000-	.00000-	.00002	.02977	.10992
74 02	1.00	.02-	67.50	.01	.00007	.00000-	.01144-	.12882	.01950	.11901
74 03	1.00	.03-	67.50	.02	1.00129	.00000-	.02000-	.33544	.00070	.12078
74 04	1.00	.04-	67.50	.03	1.61031	.00000-	.03000-	.32707	.01049-	.10537
74 05	1.00	.05-	67.50	.04	2.10000	.00000-	.04000-	.27039	.00000-	.08451
74 06	1.00	.06-	67.50	.05	2.47004	.00000-	.05000-	.24821	.05256-	.07118
74 07	1.00	.07-	67.50	.06	.00051	.00000-	.06000-	.01000	.02401	.11573
75 01	0.90	.00	67.50	.00	.00000	.00000-	.00000-	.00000	.03041	.06928
75 02	0.90	.01-	67.50	.01	.62077	.00000-	.01000-	.16011	.02617	.09751
75 03	0.90	.02-	67.50	.02	1.02923	.00000-	.02000-	.30979	.00775	.09978
75 04	0.90	.03-	67.50	.03	1.50000	.00000-	.03000-	.33000	.01463-	.08800
75 05	0.90	.04-	67.50	.04	2.04551	.00000-	.04000-	.09739	.05271-	.06697
75 06	0.90	.05-	67.50	.05	2.29000	.00000-	.05000-	.00000	.05921-	.05680
75 07	0.90	.06-	67.50	.06	.00075	.00000-	.06000-	.00000	.02727	.09121
76 01	0.80	.00	67.50	.00	.01095-	.00000-	.00000-	.00702	.03073	.07966
76 02	0.80	.01-	67.50	.01	.50000	.00000-	.01000-	.15710	.00000	.08870
76 03	0.80	.02-	67.50	.02	.90001	.00000-	.02000-	.33000	.01789	.09469
76 04	0.80	.03-	67.50	.03	1.40047	.00000-	.03000-	.40753	.00000	.08497
76 05	0.80	.04-	67.50	.04	1.90000	.00000-	.04000-	.40000	.01230-	.06406
76 06	0.80	.05-	67.50	.05	2.40000	.00000-	.05000-	.40000	.01227-	.05566
76 07	0.80	.06-	67.50	.06	2.90000	.00000-	.06000-	.40000	.01227-	.05566

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77	02	1.25	.00	90.00	.01	.01851	.00007	.01405-	.06430	.01748	.25348
77	03	1.25	6.14	90.00	.02	.60085	.71752-	.00057-	.06582	.02306	.27967
77	04	1.25	12.26	90.00	.02	1.11340	1.12145-	.04186	.01888-	.09863	.29236
77	05	1.25	16.43	90.00	.02	1.63315	1.70312-	.12777	.18565-	.02216-	.29875
77	06	1.25	20.70	90.00	.03	2.42333	1.64315-	.18222	.28857-	.02144-	.29752
77	07	1.25	22.93	90.00	.04	2.92302	1.76230-	.15345	.29644-	.00565	.29305
77	08	1.25	.00	90.00	.01	.02221	.00911-	.01917-	.07475	.01259	.25824
78	02	1.00	.01-	90.00	.00	.00420	.00300-	.00239	.00410-	.02692	.11116
78	03	1.00	6.10	90.00	.01	.57739	.59952-	.00187	.02416	.02554	.11209
78	04	1.00	12.19	90.00	.01	.99037	1.11520-	.04139	.02247-	.01189	.11665
78	05	1.00	16.29	90.00	.02	1.46951	1.01000-	.11858	.16596-	.00319	.10881
78	06	1.00	20.42	90.00	.02	2.04436	2.09212-	.20356	.36044-	.00279	.09573
78	07	1.00	22.55	90.00	.02	2.33253	2.06122-	.23490	.42465-	.02539	.08915
78	08	1.00	.00	90.00	.00	.00000	.00017	.00433	.00550-	.01541	.11653
79	02	0.50	.02-	90.00	.00	.00080	.00024-	.00044	.00009-	.03361	.08914
79	03	0.50	6.06	90.00	.01	.57172	.62302-	.00176-	.03475	.03261	.09483
79	04	0.50	12.16	90.00	.01	.96931	1.14151-	.01860	.02121	.02082	.09579
79	05	0.50	16.24	90.00	.02	1.41314	1.62233-	.08520	.10843-	.01480	.08744
79	06	0.50	20.37	90.00	.02	1.90980	2.00003-	.17945	.30335-	.01790	.07837
79	07	0.50	22.44	90.00	.03	2.16033	2.06129-	.15067	.29672-	.03617	.07579
79	08	0.50	.01-	90.00	.00	.00032	.00016	.00257	.00446-	.02755	.09617
80	02	0.60	.01-	90.00	.00	.01085-	.02532	.00880-	.00692	.03936	.07768
80	03	0.60	6.04	90.00	.00	.53740	.60905-	.01708-	.04360	.04258	.08241
80	04	0.60	12.11	90.00	.00	.90125	1.12142-	.00305	.00077	.03146	.08414
80	05	0.60	16.13	90.00	.00	1.29971	1.62591-	.03541	.06312-	.03276	.07870
80	06	0.60	20.20	90.00	.00	1.70750	2.10125-	.10666	.23071-	.03404	.07514
80	07	0.60	22.23	90.00	.00	1.91375	2.24080-	.12956	.23733-	.04283	.06796
80	08	0.60	.02-	90.00	.00	.00410-	.01195	.00879-	.00689	.03938	.07807

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31	32	1.25	.01	112.50	.01	.0222	.01250	.01778-	.05475	.02000	.25339
31	04	1.25	12.28	112.50	.05-	1.15277	1.33132-	.10563	.45067-	.03235	.29709
31	03	1.25	16.41	112.50	.09-	1.64135	1.62235-	.22067	.89042-	.06783	.30637
31	06	1.25	20.56	112.50	.12-	2.42009	1.90961-	.24763	.04754-	.07271	.31247
31	07	1.25	22.88	112.50	.12-	3.01145	2.17506-	.22012	.98065-	.09579	.30736
31	08	1.25	25.14	112.50	.01-	.70771	.82044-	.52728	.13261-	.01936	.28763
31	09	1.25	.01	112.50	.01	.02501	.00033-	.01585-	.06525	.31521	.25939
32	03	1.00	.01-	112.50	.00	.00503	.00827-	.00449-	.01095-	.02989	.11095
32	03	1.00	9.10	112.50	.02-	.61067	.73662-	.03840	.16305-	.02992	.11565
32	04	1.00	12.20	112.50	.05-	1.05195	1.42954-	.13495	.52697-	.03585	.11853
32	06	1.00	16.26	112.50	.09-	1.52948	2.01097-	.24562	.98288-	.07067	.11944
32	07	1.00	20.33	112.50	.08-	2.00571	2.43194-	.27202	.99655-	.12919	.11260
32	08	1.00	22.50	112.50	.08-	2.25505	2.59540-	.26871	.01898-	.16065	.10147
32	09	1.00	.01-	112.50	.00	.00844	.01683-	.00852	.01131-	.02095	.11106
33	01	0.90	.01-	112.50	.00	.01003	.01926-	.00246	.00438-	.01807	.09441
33	02	0.90	9.06	112.50	.02-	.59452	.75842-	.02837	.14579-	.02462	.10030
33	03	0.90	12.15	112.50	.05-	1.01875	1.42508-	.11691	.50035-	.03106	.10635
33	04	0.90	15.21	112.50	.09-	1.44100	1.93955-	.22168	.92225-	.07825	.10670
33	05	0.90	20.33	112.50	.07-	1.88905	2.24370-	.18455	.79617-	.16003	.10003
33	06	0.90	22.41	112.50	.07-	2.17549	2.53115-	.17996	.75471-	.18199	.09122
33	07	0.90	.02-	112.50	.00	.01546	.02965-	.00199-	.00180	.01800	.09384
34	03	0.60	.01-	112.50	.00	.00425-	.01185	.00890-	.00700	.03088	.08072
34	04	0.60	9.05	112.50	.01-	.56409	.73021-	.01579	.14043-	.03545	.08734
34	05	0.60	12.08	112.50	.03-	.92558	1.34255-	.08403	.41091-	.04334	.09271
34	06	0.60	16.12	112.50	.06-	1.34701	2.01057-	.20721	.89132-	.06902	.09561
34	07	0.60	20.17	112.50	.09-	1.75197	2.55434-	.26355	.23181-	.14665	.08967
34	08	0.60	22.22	112.50	.09-	1.99600	2.92266-	.22366	.11139-	.12640	.08748
34	09	0.60	.01-	112.50	.00	.00361-	.01146	.01193-	.00929	.03508	.07975

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00	1.25	00	135.00	00	02795	00310	02854-	07726	02485	24972
01	1.25	01	135.00	01	72985	97307-	00940-	00412-	03728	28598
02	1.25	01	135.00	01	1.20144	1.61444-	01020	07635-	03453	30174
03	1.25	03	135.00	03	1.75261	2.13924-	04957	25590-	03570	30730
04	1.25	04	135.00	04	2.61112	2.75357-	04151	25379-	02209	30195
05	1.25	04	135.00	04	3.11285	2.91396-	0143-	13790-	04535	29377
06	1.25	00	135.00	00	03245	00685-	02477-	06464	01741	25357
07	1.00	01	135.00	00	00079	00045-	00036	00006	02682	11043
08	1.00	01	135.00	01	62776	8944E-	01245	07737-	03615	12033
09	1.00	02	135.00	02	1.11015	1.79236-	03016	14004-	03857	12680
10	1.00	03	135.00	03	1.55500	2.72394-	06551	29452-	05219	11952
11	1.00	05	135.00	05	2.25015	3.49853-	10150	44374-	06428	10084
12	1.00	06	135.00	06	2.59905	3.78564-	09461-	07300-	05196	08241
13	1.00	00	135.00	00	00529	00922-	00026	00241-	02132	11858
14	0.90	01	135.00	00	00093	01026-	00028	00275-	02132	09547
15	0.90	01	135.00	01	62457	92854-	00925	07475-	02641	10784
16	0.90	02	135.00	02	1.09000	1.84990-	02219	13520-	03744	11255
17	0.90	03	135.00	03	1.50123	2.77673-	04532	27109-	04914	10630
18	0.90	03	135.00	03	2.12612	3.61110-	00404-	12455-	06139	08535
19	0.90	01	135.00	01	2.59214	3.85113-	06477-	07841	05392	07650
20	0.90	00	135.00	00	00548	01600-	00249	00457-	01658	09980
21	0.60	00	135.00	00	00521	01449-	00505-	00467	02649	07970
22	0.60	01	135.00	01	55632	89929-	00466-	05115-	03979	08803
23	0.60	01	135.00	01	1.02050	1.71641-	01021	11505-	03891	09741
24	0.60	02	135.00	02	1.48945	2.04177-	03390	23622-	05051	09439
25	0.60	03	135.00	03	1.96644	3.55455-	04538	32279-	06564	08021
26	0.60	03	135.00	03	2.23184	3.99943-	00261	18960-	07470	07168
27	0.60	00	135.00	00	00277	00219-	01195-	01316	03059	07771

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89 02	1.25	.00	157.50	.00	.02295	.00254	.02149-	.05842	.02007	.25363
89 03	1.25	.016	157.50	.01	.71737	.37862-	.05052-	.14569	.03875	.28338
89 04	1.25	12.25	157.50	.04	1.13239	1.37752-	.11768-	.45243	.02882	.29917
89 05	1.25	13.35	157.50	.03	1.64922	1.75240-	.19358-	.75310	.01389-	.30520
89 06	1.25	20.66	157.50	.09	2.49242	2.25373-	.21761-	.86570	.05286-	.30380
89 07	1.25	22.43	157.50	.09	2.95765	2.44716-	.20883-	.82812	.07498-	.29786
89 08	1.25	.01	157.50	.00	.05166	.01264-	.02156-	.05355	.01525	.25842
90 02	1.00	.01-	157.50	.00	.00502	.00307-	.00251	.00159-	.03264	.10943
90 03	1.00	8.08	157.50	.00	.60472	.82828-	.01589-	.03519	.02796	.11353
90 04	1.00	12.15	157.50	.03	1.01927	1.46515-	.05832-	.35744	.03500	.11734
90 05	1.00	13.24	157.50	.07	1.48935	2.07524-	.17036-	.73434	.00777	.11528
90 06	1.00	20.49	157.50	.07	1.97237	2.39077-	.17906-	.73277	.04522-	.09744
90 07	1.00	22.47	157.50	.07	2.31135	2.59322-	.18129-	.75391	.06063-	.08695
90 08	1.00	.01-	157.50	.00	.00469	.01478-	.00445	.00301-	.02102	.11352
91 01	0.90	.01-	157.50	.00	.01032	.01972-	.00028	.00007	.02125	.09514
91 02	0.90	8.09	157.50	.00	.51536	.37827-	.02362-	.00685	.03329	.09917
91 03	0.90	12.15	157.50	.03	1.00026	1.49759-	.11131-	.42694	.02715	.10477
91 04	0.90	16.20	157.50	.06	1.58571	1.69055-	.17440-	.71021	.01779-	.10286
91 05	0.90	20.30	157.50	.06	1.81934	2.21646-	.15783-	.65676	.05469-	.09154
91 06	0.90	22.38	157.50	.06	2.09685	2.45162-	.16395-	.66302	.07773-	.07735
91 08	0.90	.01-	157.50	.00	.01537	.02982-	.00191-	.00455	.02126	.09624
92 02	0.60	.01-	157.50	.00	.00189	.00107-	.00578-	.00462	.03087	.03084
92 03	0.60	5.07	157.50	.00	.56243	.79570-	.04714-	.10568	.04322	.08593
92 04	0.60	12.03	157.50	.02	.92251	1.42419-	.11650-	.39464	.04397	.09058
92 05	0.60	16.12	157.50	.04	1.34756	2.07685-	.20920-	.76350	.02653	.08930
92 07	0.60	20.16	157.50	.07	1.75474	1.67420-	.29153-	.17428	.00500-	.07869
92 08	0.60	22.21	157.50	.06	2.01569	2.39461-	.32451-	.31296	.01842-	.07056
92 09	0.60	.01-	157.50	.00	.00306	.00186-	.01195-	.00327	.03503	.07618

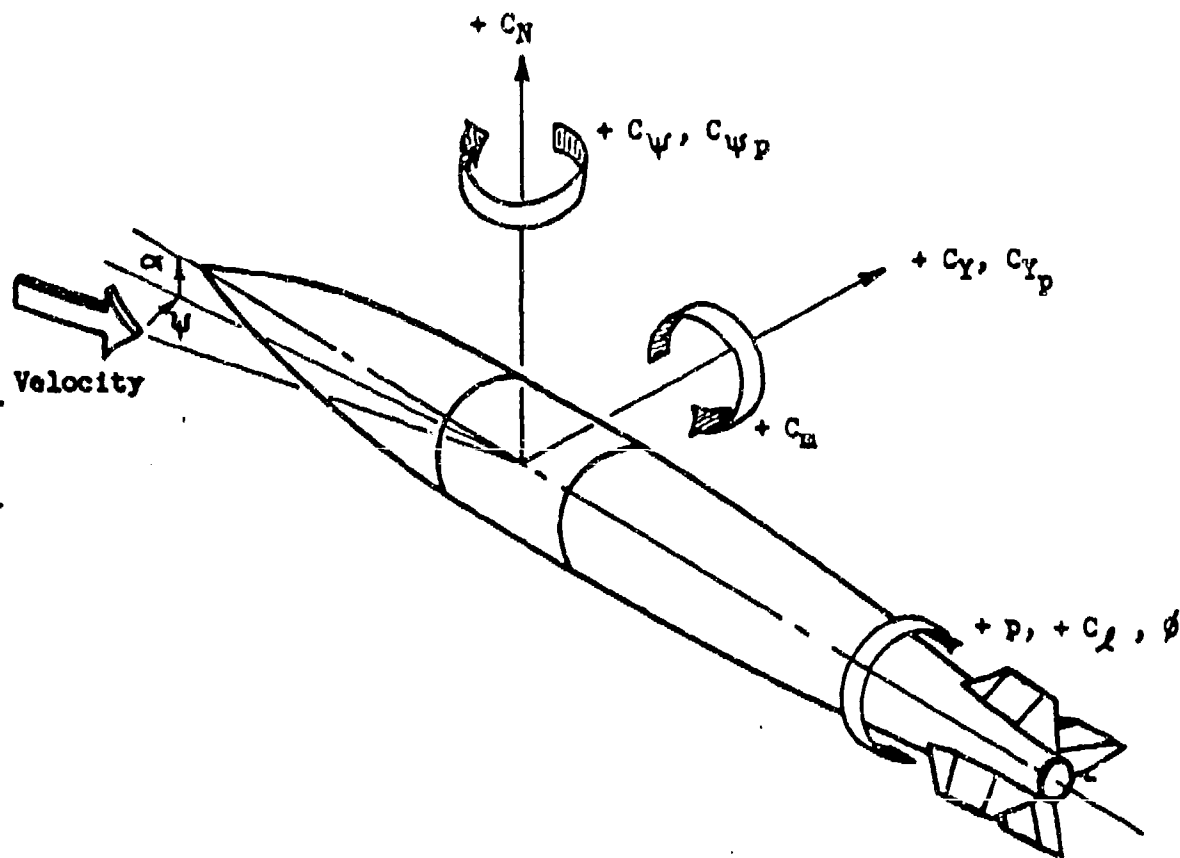
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92 02	1.25	.00	180.00	.00	.02257	.00033	.02130-	.04666	.02011	.25496
92 03	1.25	6.15	180.00	.00	.68352	.75502-	.02312-	.07175	.03227	.27747
92 04	1.25	12.27	180.00	.00	1.09741	1.16893-	.04024-	.08840	.02419	.28799
92 05	1.25	16.40	180.00	.00	1.52626	1.41592-	.04397-	.10352	.02155	.29470
92 06	1.25	20.70	180.00	.00	2.41425	1.77779-	.04029-	.07365	.00269-	.29217
92 08	1.25	.00	180.00	.00	.03092	.01114-	.01550-	.03761	.01274	.25779
94 02	1.20	.00	180.00	.01-	.04520	.09303-	.01110	.03321-	.02366	.25104
94 03	1.20	3.11	180.00	.02-	.72062	1.00013-	.01070	.10102-	.04049	.27173
94 04	1.20	12.22	180.00	.02-	1.13578	1.46865-	.01246	.11490-	.03681	.28579
94 05	1.20	16.38	180.00	.02-	1.61603	1.73917-	.01633	.13028-	.02630	.29057
94 06	1.20	20.60	180.00	.02-	2.35745	1.09245-	.00254-	.07534-	.01928	.28353
94 07	1.20	22.78	180.00	.01-	2.88344	2.32879-	.03633-	.03693	.01740	.27671
94 08	1.20	.00	180.00	.01-	.04455	.10223-	.01475	.08843-	.01848	.25441
95 01	1.10	.00	180.00	.00	.00429	.36722	.00727	.00275-	.02021	.25513
95 02	1.10	6.15	180.00	.00	.64099	.55263-	.01475	.03614-	.03083	.26043
95 03	1.10	12.22	180.00	.00	1.03960	1.14180-	.00445-	.00022	.03214	.26745
95 04	1.10	16.35	180.00	.01-	1.52697	1.54400-	.01574	.05560-	.02472	.27474
95 05	1.10	20.52	180.00	.02-	2.07460	1.63857-	.03554	.15651-	.01340	.28051
95 06	1.10	22.66	180.00	.02-	2.51735	1.72527-	.05477	.20966-	.00411	.28000
95 07	1.10	.00	180.00	.00	.00342	.07734	.00778	.00227	.01464	.25603

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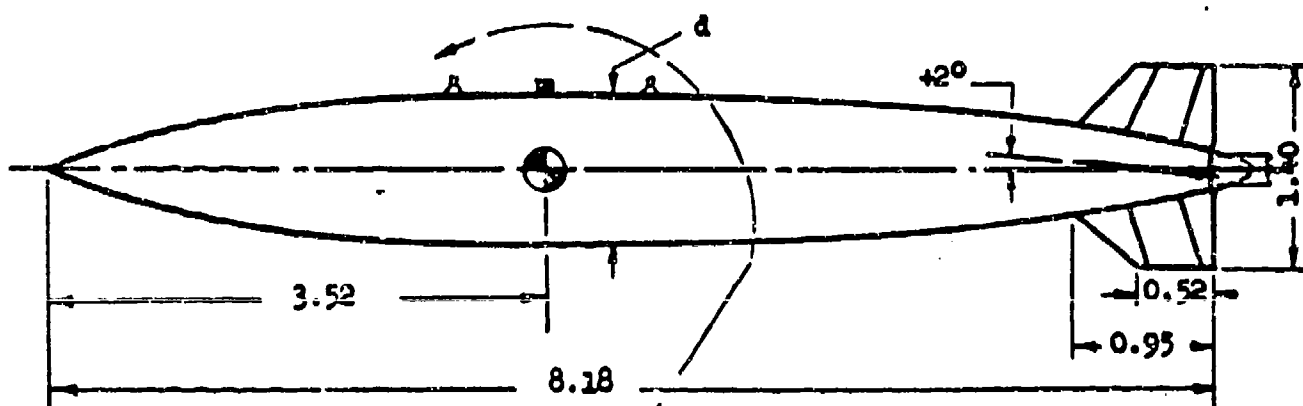
96 02	1.00	.01-	125.00	.00	.00339-	.00262	.00042	.00001	.02972	.10902
96 03	1.00	3.09	130.00	.00	.52273	.70708-	.00417	.02449-	.04054	.10754
96 04	1.00	12.16	180.00	.01-	.96525	1.25474-	.00077	.03275-	.03584	.10430
96 05	1.00	16.27	100.00	.00	1.43327	1.00983-	.00095	.03281-	.02747	.10037
96 06	1.00	20.40	180.00	.01-	1.96050	2.14153-	.00498	.05332-	.01523	.08336
96 07	1.00	22.49	155.00	.02-	2.22520	2.20475-	.03267	.16111-	.00075	.07626
96 08	1.00	.01-	180.00	.00	.00079	.00043-	.00036	.00000	.02673	.10992
97 01	0.90	.01-	180.00	.00	.00580	.01056-	.00189-	.00454	.02432	.09298
97 02	0.90	8.08	180.00	.00	.56144	.71662-	.00399-	.00585-	.03594	.08806
97 03	0.90	12.13	180.00	.00	.54211	1.27053-	.00143	.02152-	.03103	.09014
97 04	0.90	15.21	180.00	.00	1.35033	1.74195-	.00696-	.00369	.02638	.08414
97 05	0.90	20.33	180.00	.01-	1.78813	1.95924-	.01796	.10314-	.00951	.07483
97 06	0.90	22.40	180.00	.02-	2.00063	2.03052-	.05069	.24068-	.00326	.06764
97 07	0.90	.00	150.00	.00	.00015	.00027-	.00260	.00112	.02431	.09404
98 02	0.00	.01-	180.00	.00	.00404	.00297-	.01805-	.01779	.03953	.07933
98 03	0.00	6.04	180.00	.00	.54390	.71296-	.01366-	.00999	.05591	.07738
98 04	0.00	12.06	180.00	.00	.88621	1.22073-	.01167-	.00347-	.05370	.08125
98 05	0.00	15.14	180.00	.00	1.27441	1.74477-	.01613-	.01116	.04615	.07518
98 06	0.00	20.18	180.00	.01-	1.60113	2.14495-	.01219-	.01577-	.02978	.07052
98 07	0.00	22.23	180.00	.01-	1.86845	2.26739-	.01063	.06859-	.02545	.06293
98 08	0.00	.00	180.00	.00	.00240	.00164-	.00071-	.01069	.04376	.07591

Coordinate Axes and Sign Convention

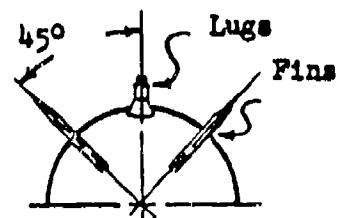
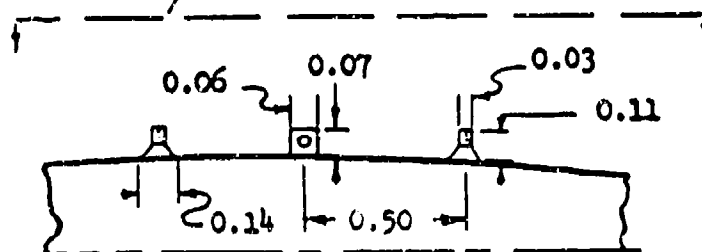


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0.214-Scale Model of the U. S. Navy
1000 lb Mk 81 Low-Drag Bomb



Note: All dimensions are in units
of maximum body diameters (d)
 $d = 3.00$ inches

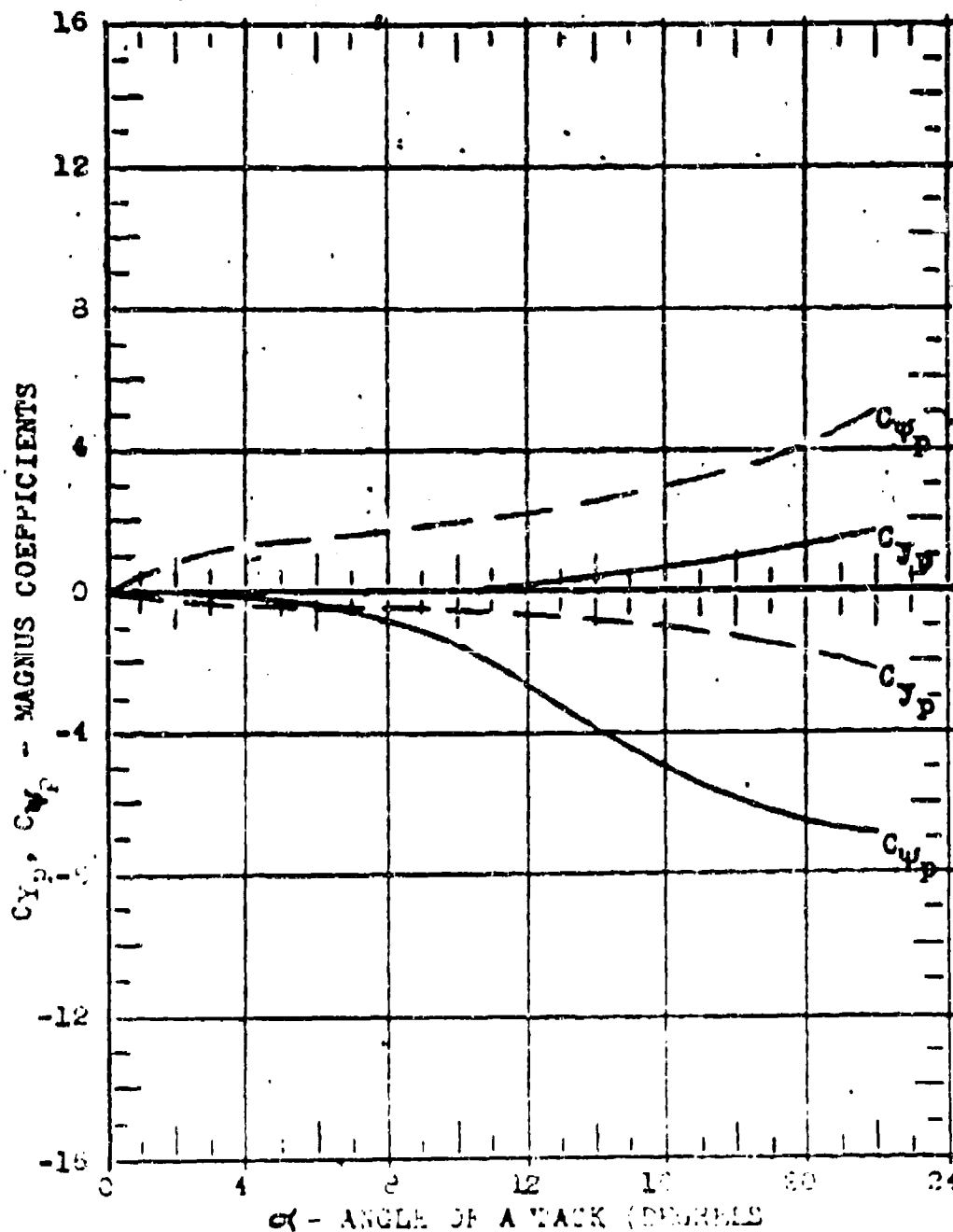


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LOW-DRAG BOMB

VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 1.25$

— $Re = 2 \times 10^6$
- - $Re = 4 \times 10^6$
— $Re = 6 \times 10^6$

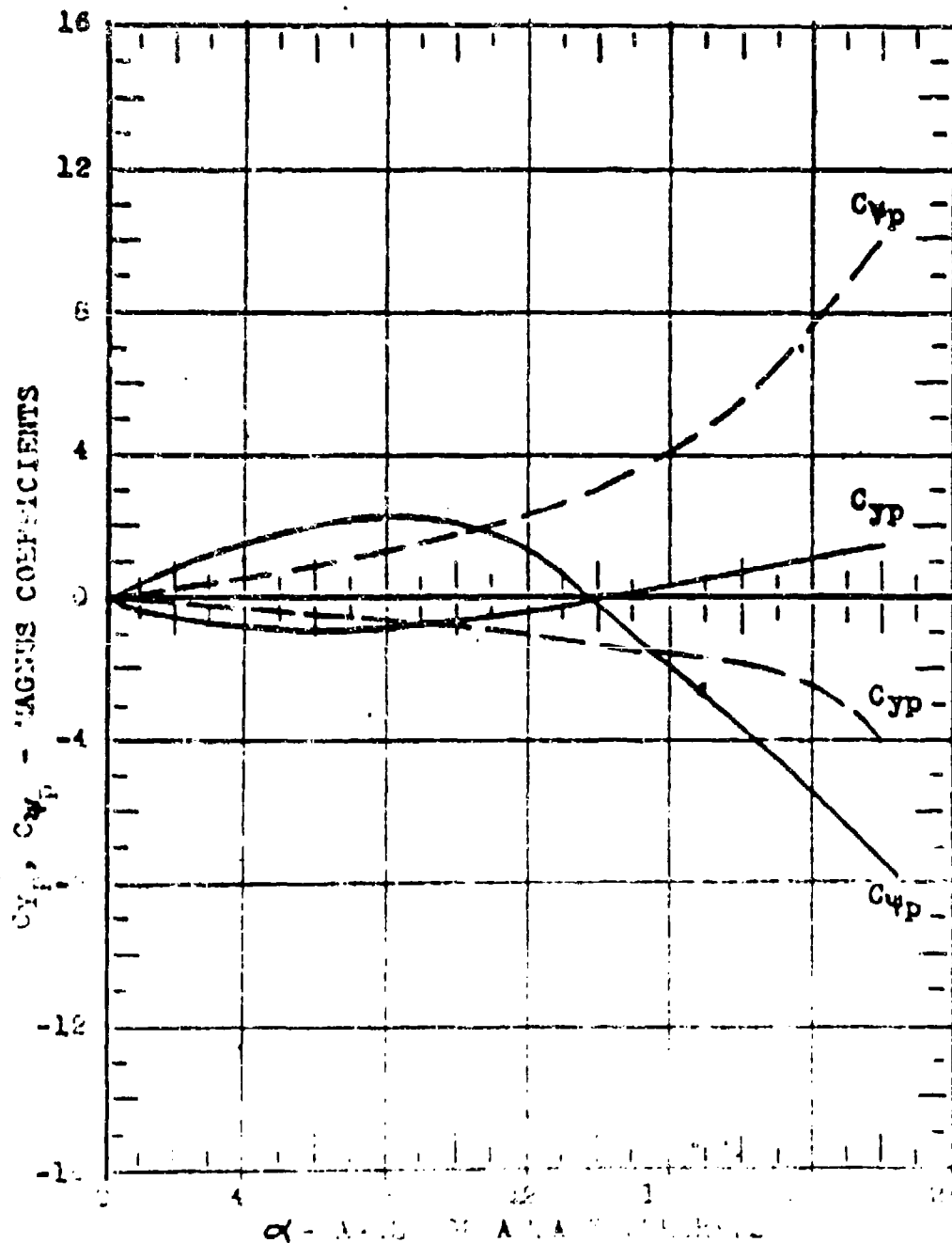


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VARIATION OF MAGNUS FORCE AND MOMENT
 COEFFICIENT WITH ANGLE OF ATTACK

$M = 1.20$

— $Re = 2 \times 10^6$
 - - $Re = 4 \times 10^6$
 — $Re = 6 \times 10^6$

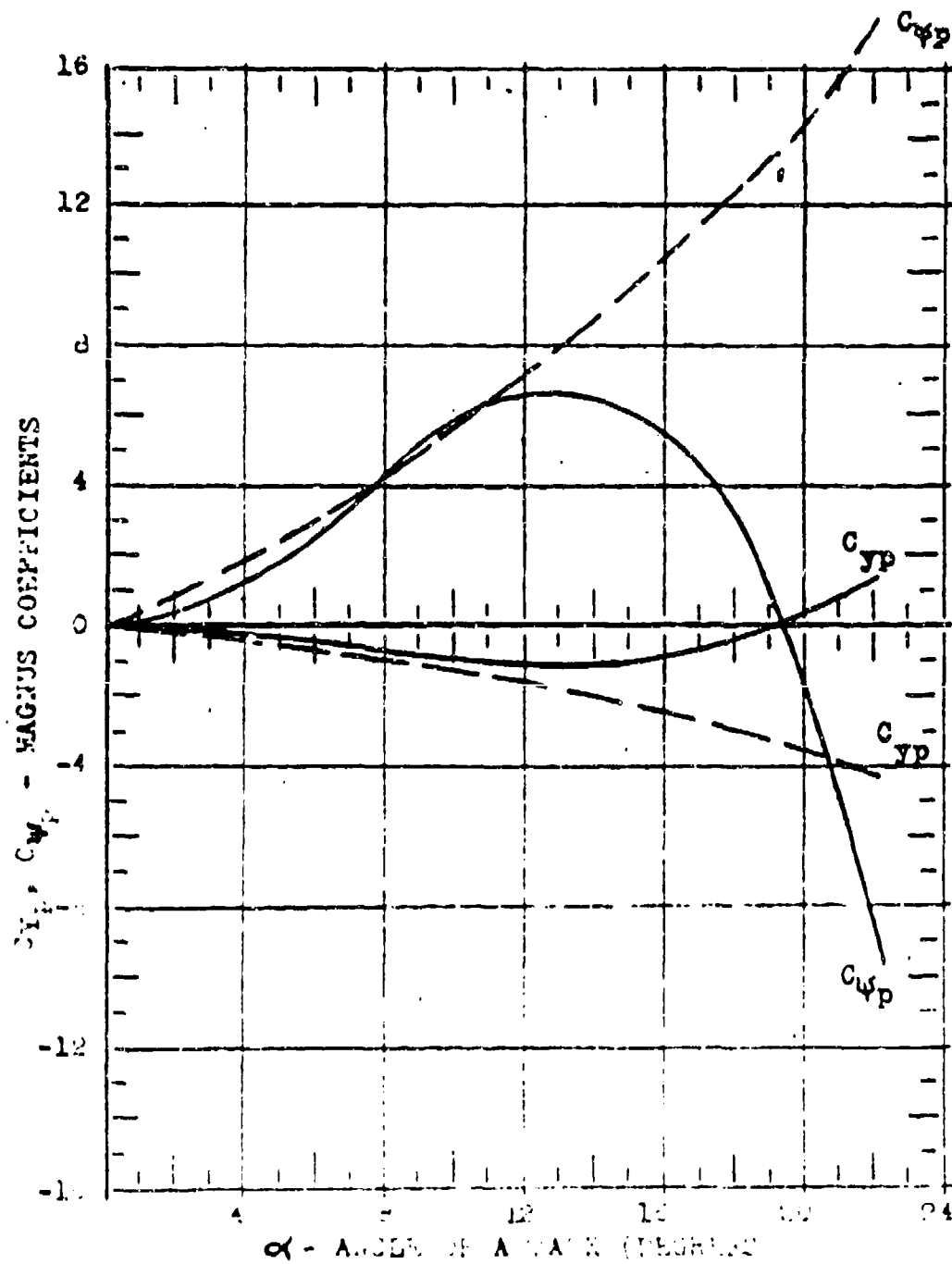


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VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 1.19$

— $Re = 2 \times 10^6$
-- $Re = 4 \times 10^6$
--- $Re = 6 \times 10^6$

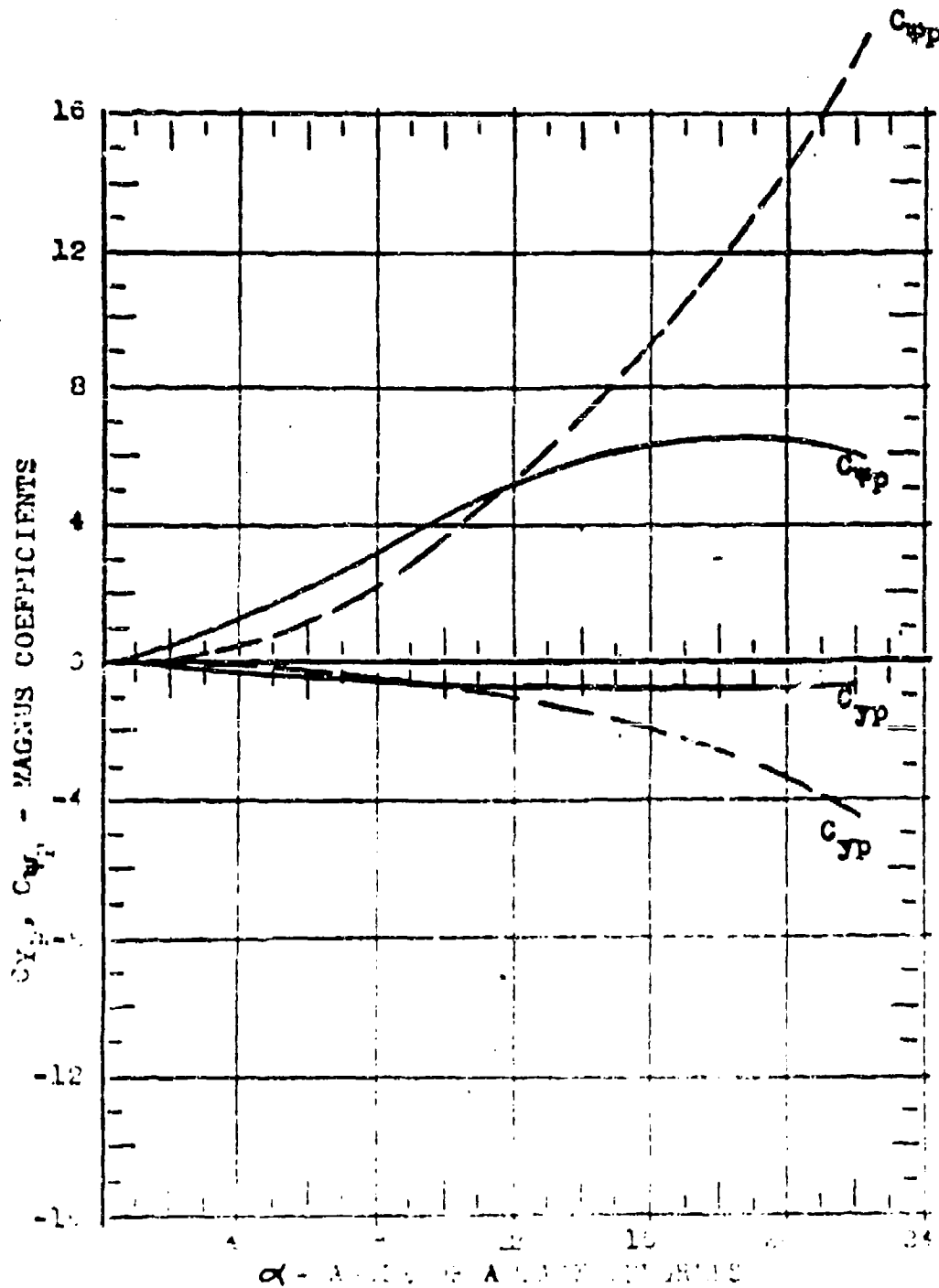


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VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 1.00$

— $Re = 2 \times 10^6$
-- $Re = 4 \times 10^6$
--- $Re = 6 \times 10^6$

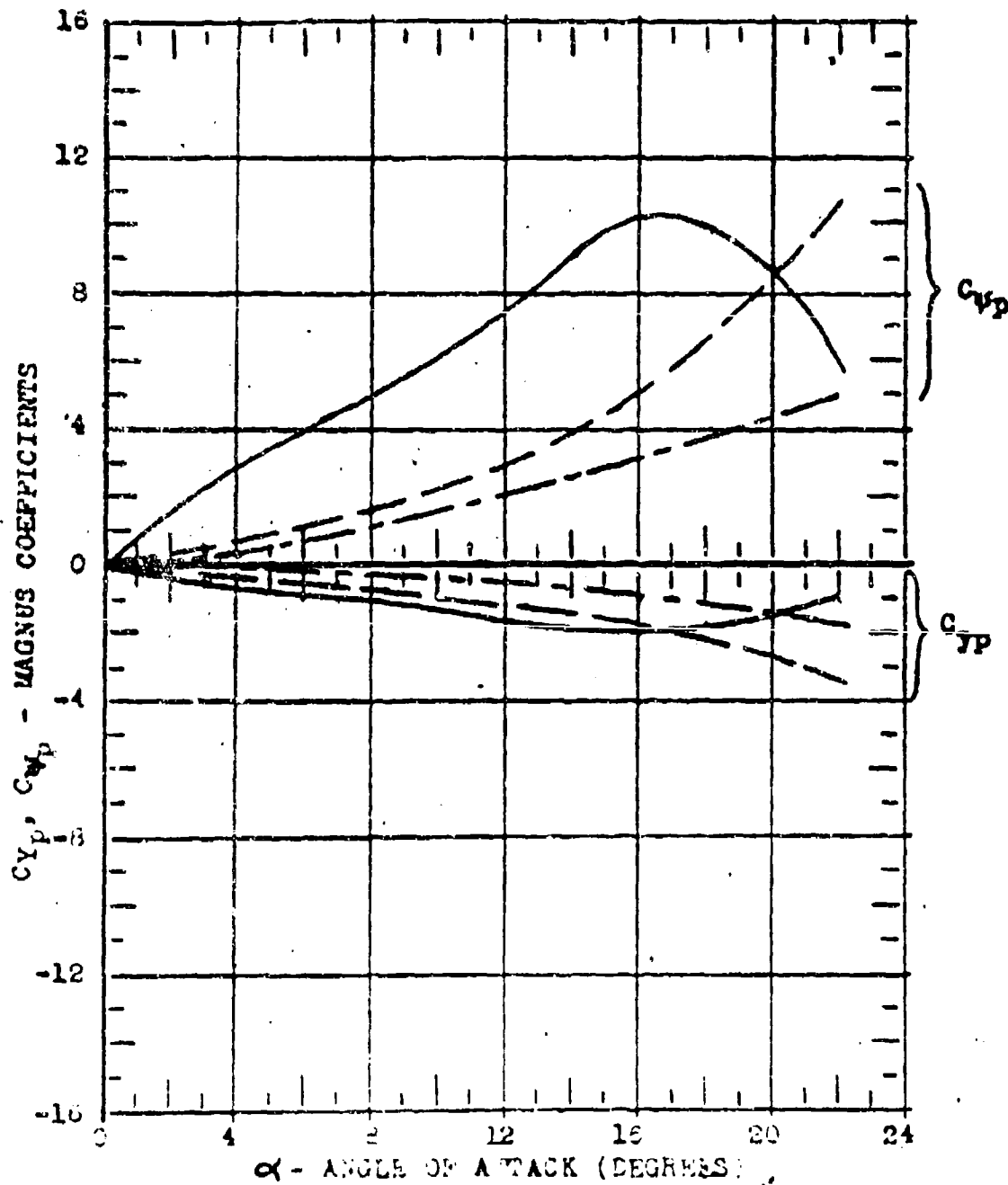


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VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 0.95$

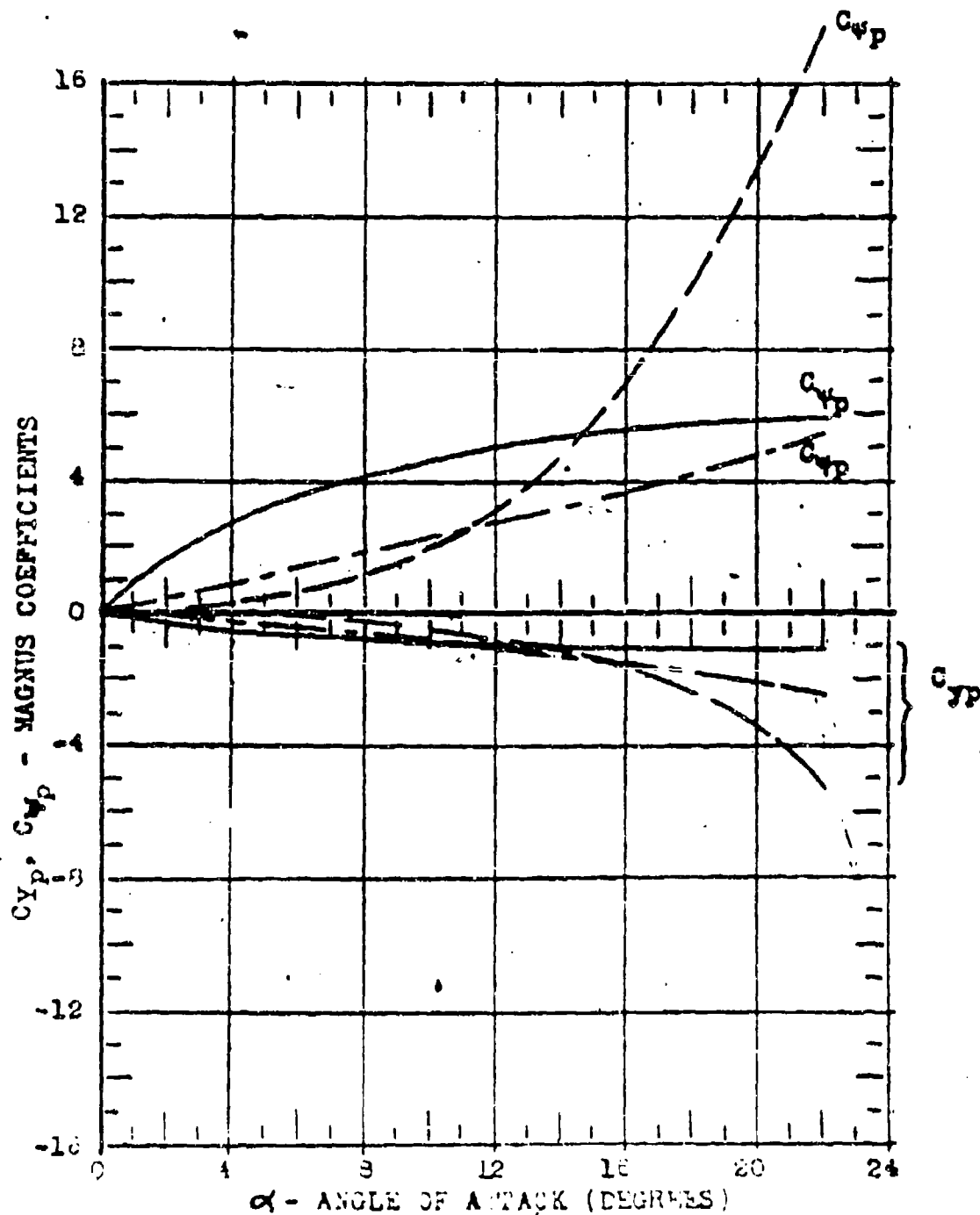
— $Re = 2 \times 10^6$
- - $Re = 4 \times 10^6$
— $Re = 6 \times 10^6$



VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 0.90$

— $Re = 2 \times 10^5$
- - $Re = 4 \times 10^5$
- - $Re = 6 \times 10^5$

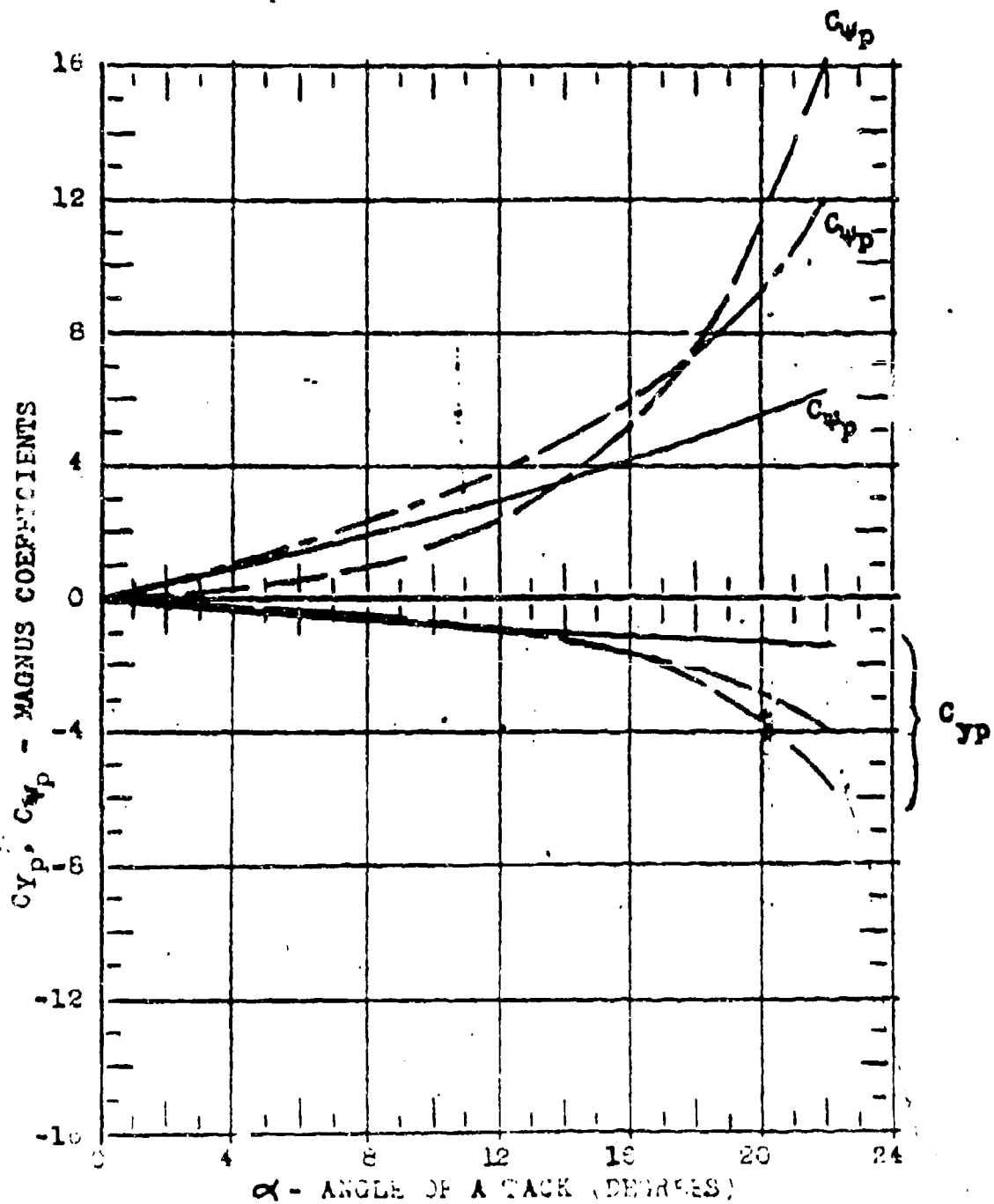


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VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 0.80$

— $Re = 2 \times 10^6$
- - $Re = 4 \times 10^6$
— $Re = 6 \times 10^6$

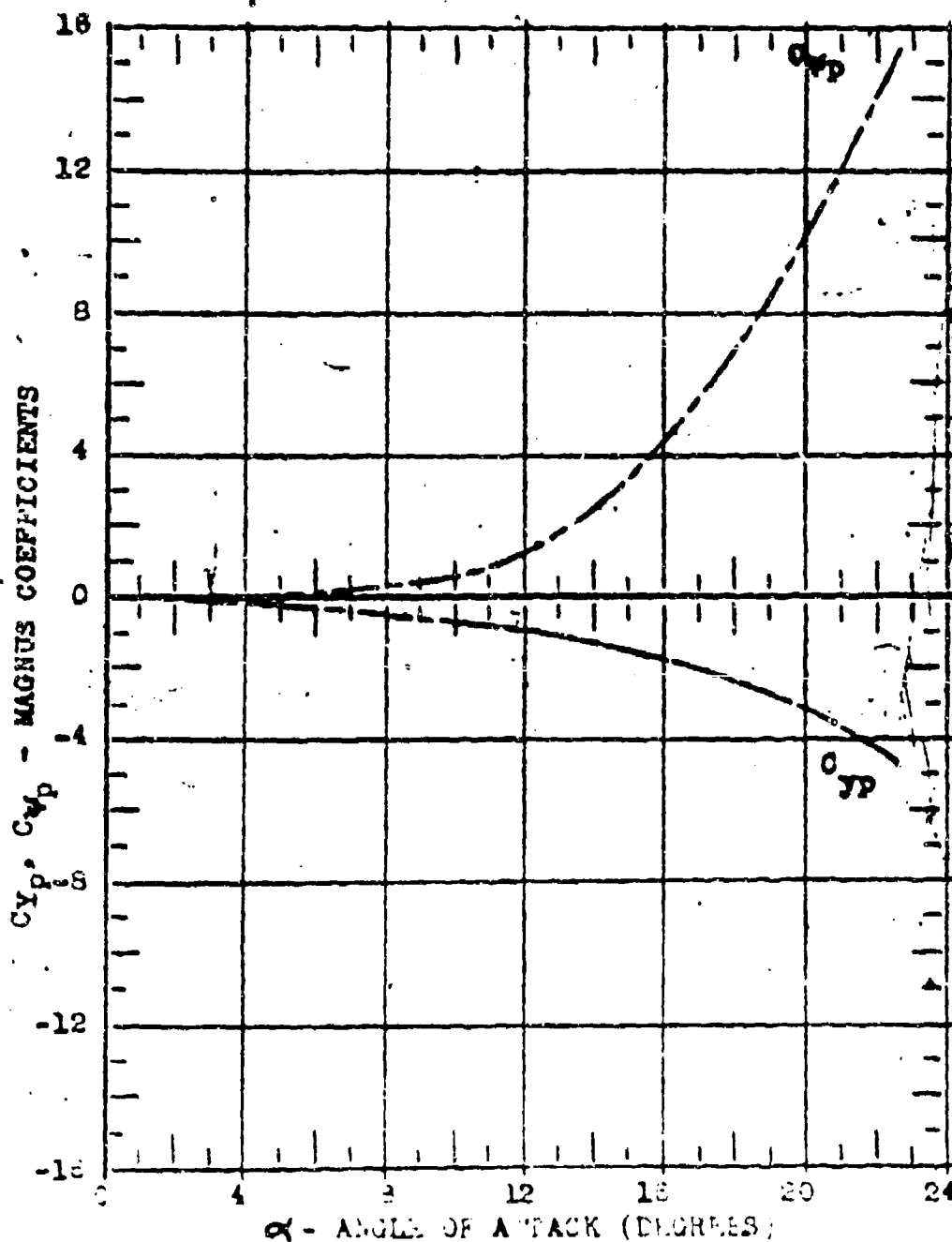


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VARIATION OF MAGNUS FORCE AND MOMENT
COEFFICIENT WITH ANGLE OF ATTACK

$M = 0.60$

— $Re = 2 \times 10^6$
- - $Re = 4 \times 10^6$
— $Re = 6 \times 10^6$



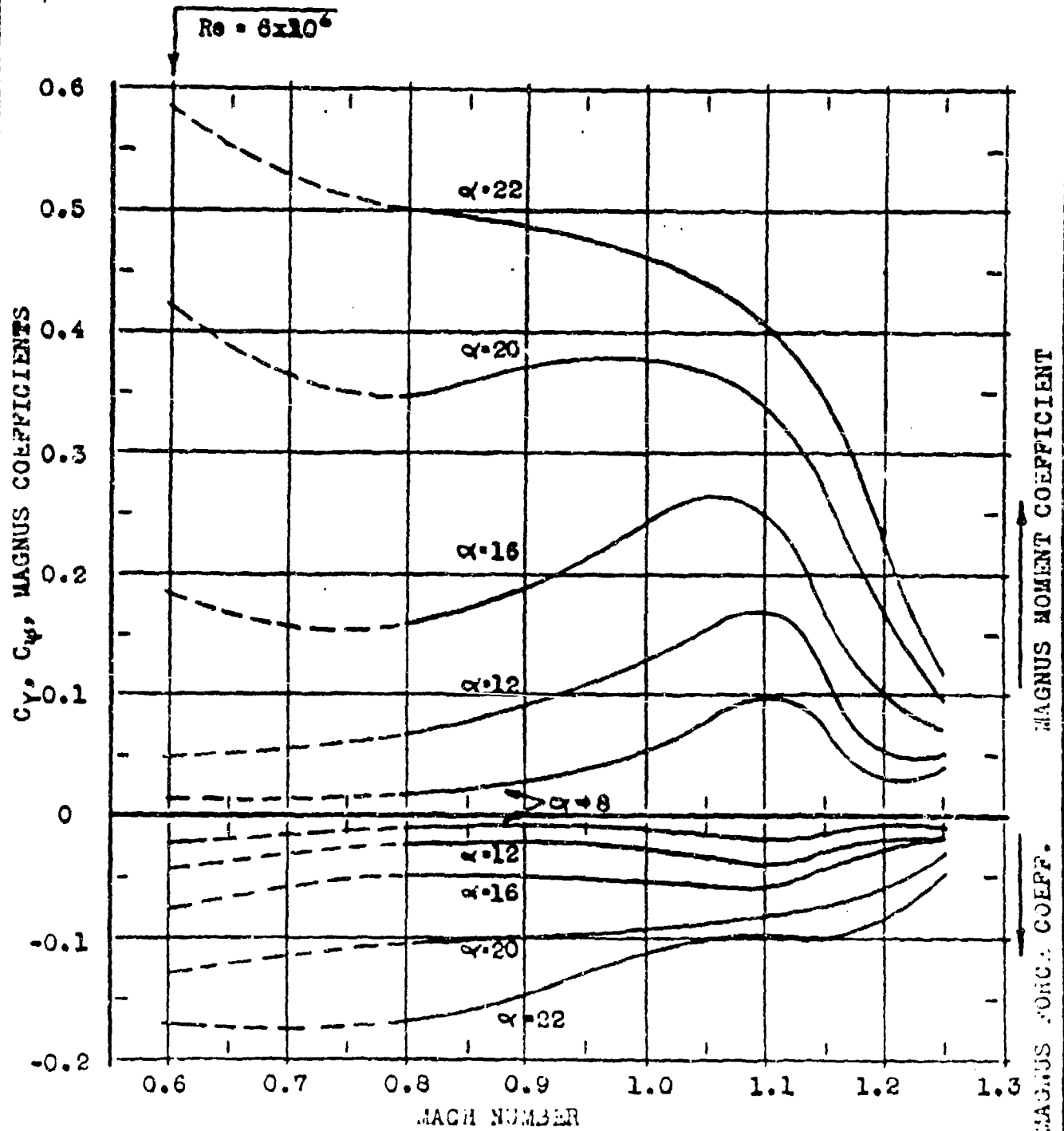
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FIGURE 12

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VARIATION OF MAGNUS FORCE AND MOMENT COEFFICIENT WITH MACH NUMBER FOR MODEL
REYNOLDS NUMBER OF 4×10^5

$p = 2000$ RPM



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FIGURE 11

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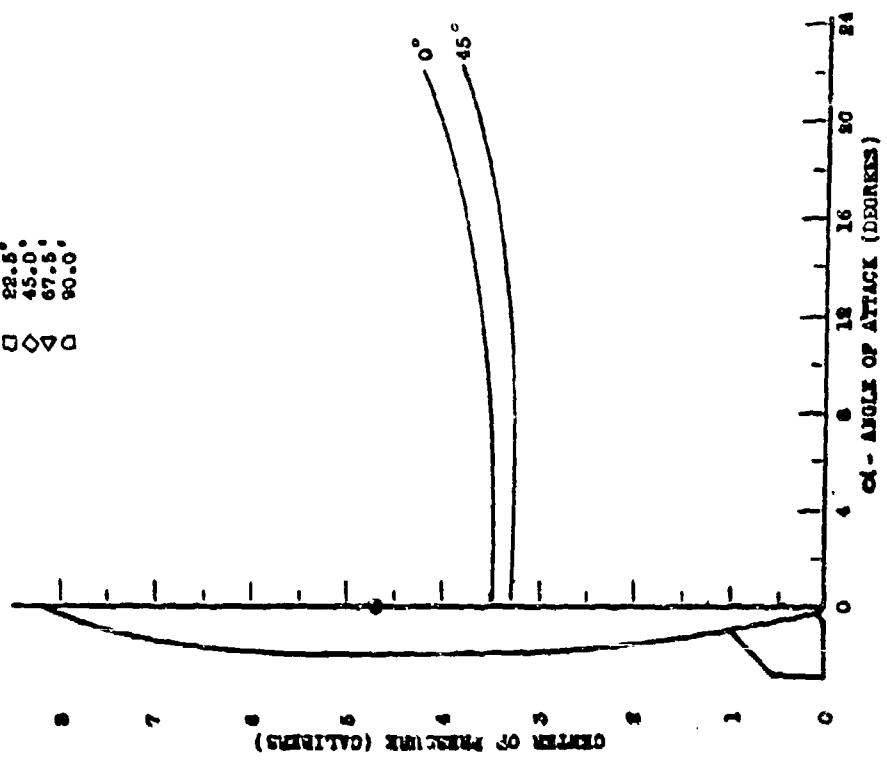
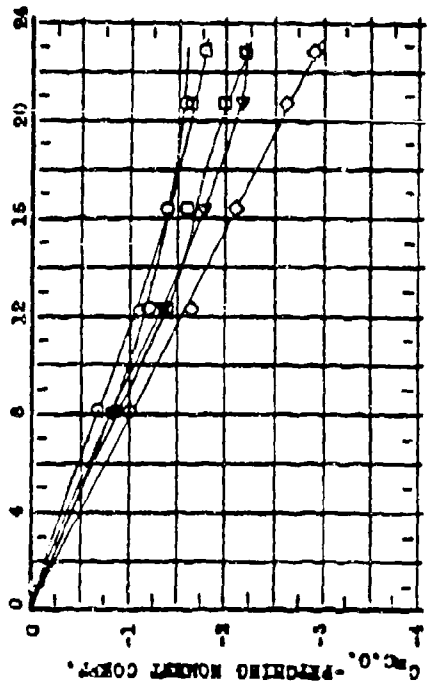
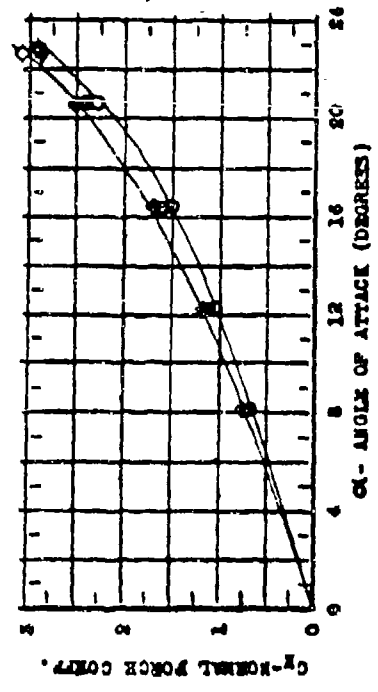
LOW-DRAG BOMB

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 1.25$

ϕ
0
22.5
45.0
67.5
90.0

□ Δ ◇ □



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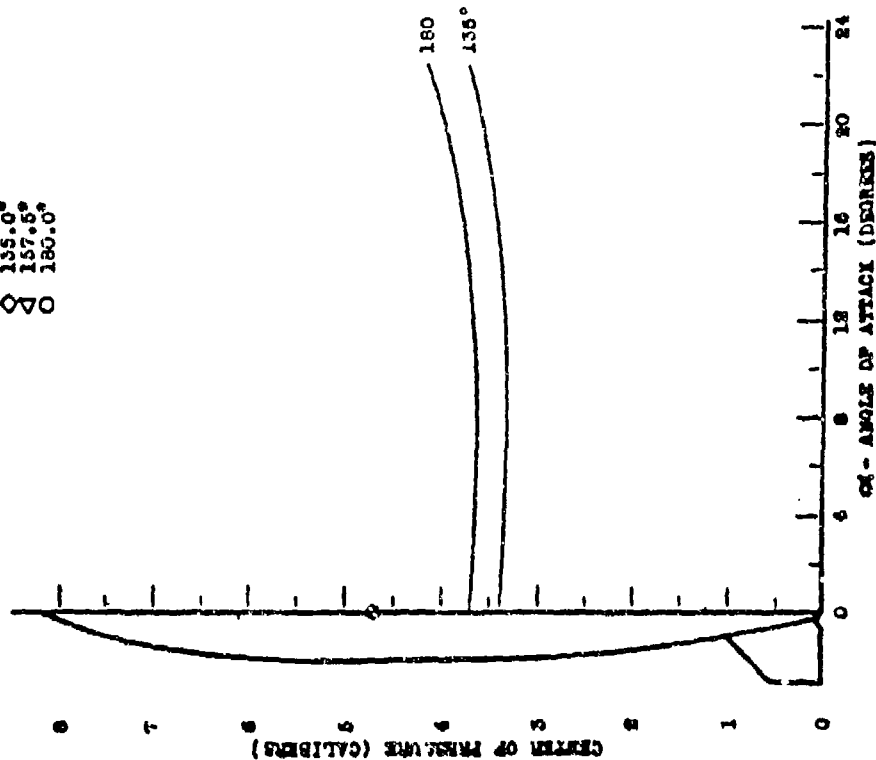
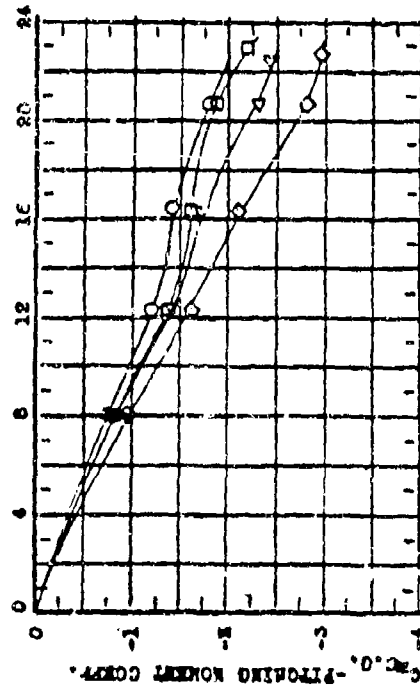
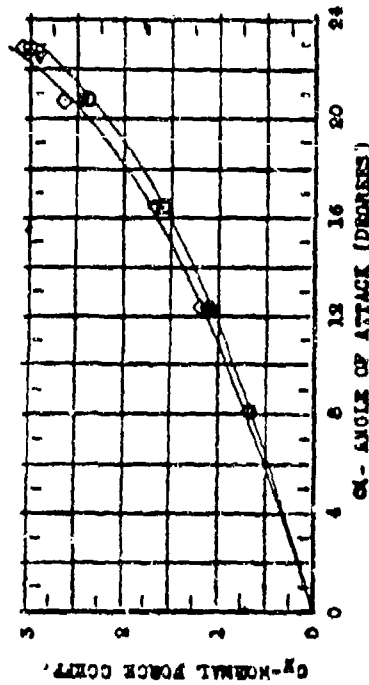
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LOW-DRAG BOMB

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENTS WITH ANGLE OF ATTACK
AT VARIOUS NOSE-ROLL ANGLES

N = 1.25

α
□ 112.5°
◇ 135.0°
△ 157.5°
○ 180.0°



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FIGURE 23

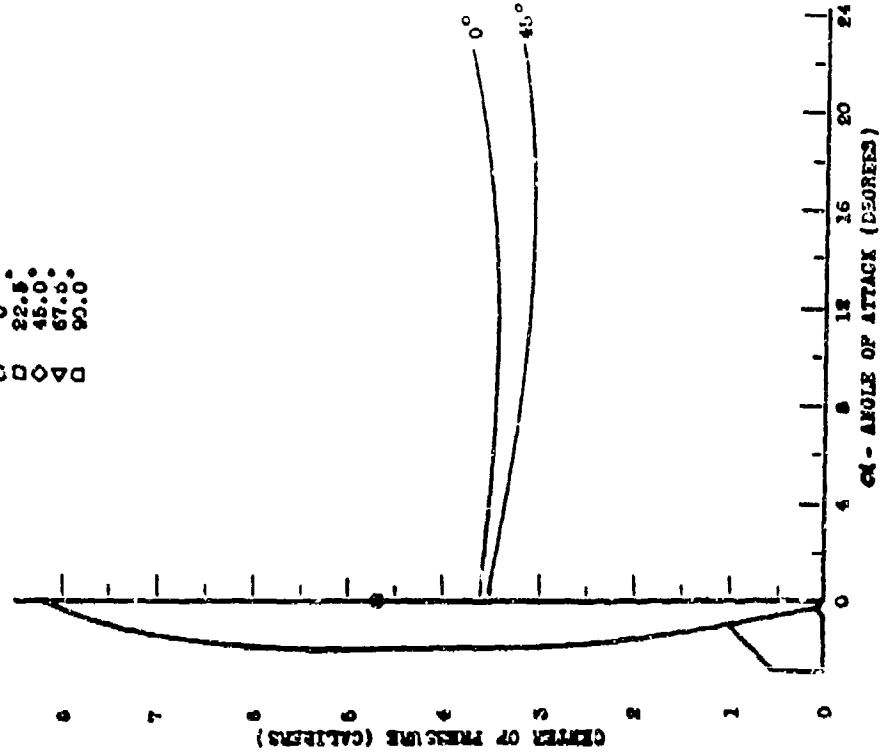
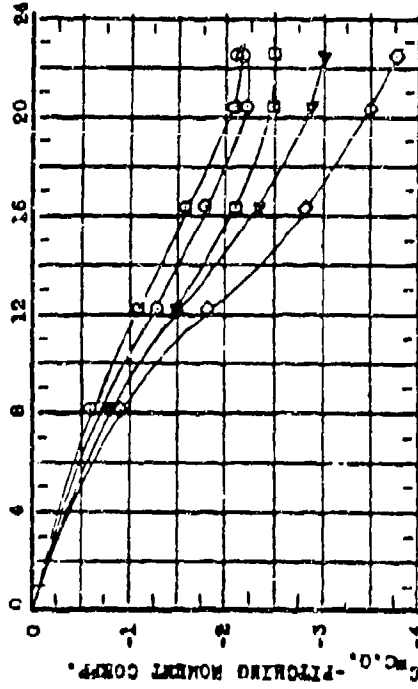
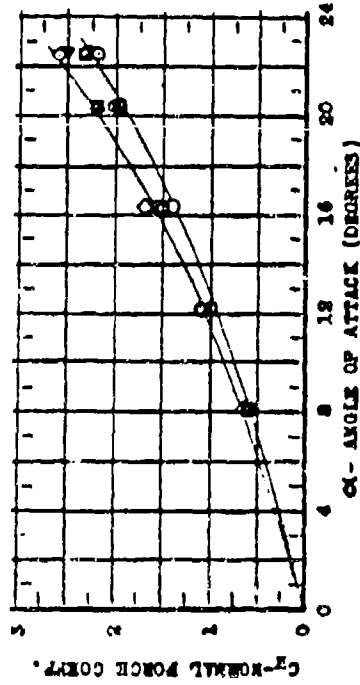
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LOW-DRAG BOMB

VARIAION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 1.00$

ϕ
0°
22.5°
45.0°
67.5°
90.0°



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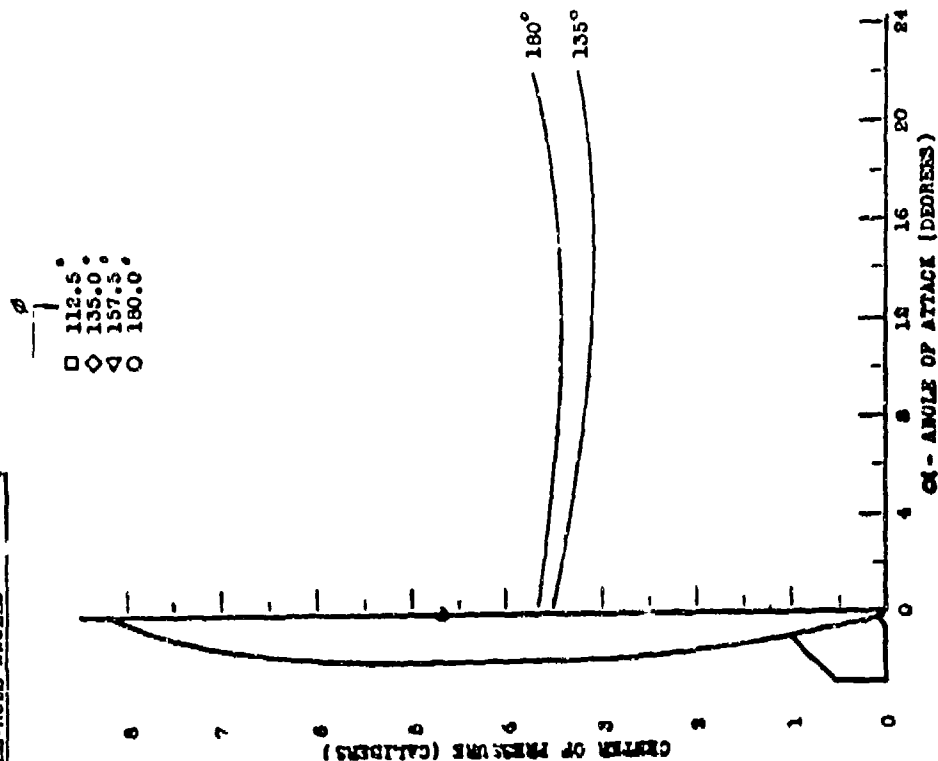
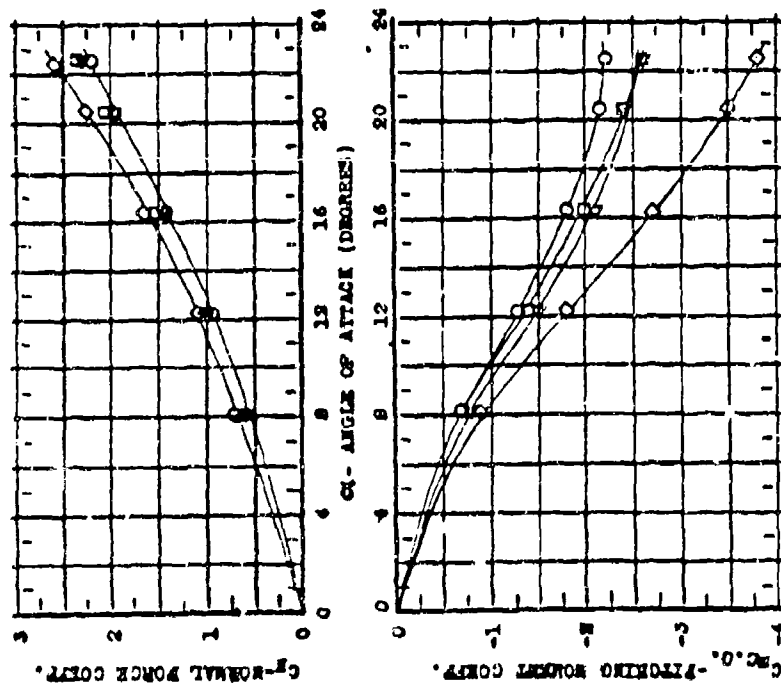
FIGURE 14

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LOW-DRAG BOX

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 1.00$



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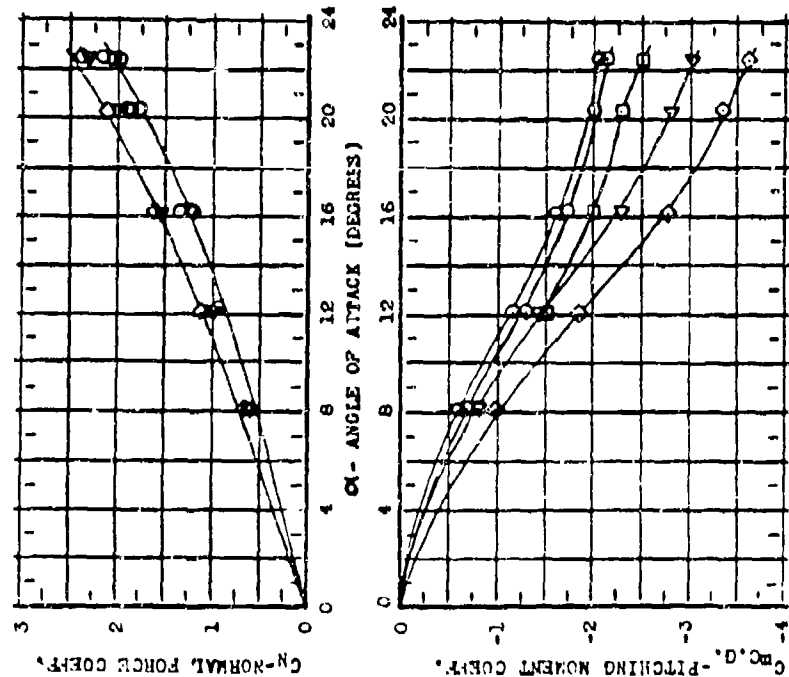
FIGURE 16

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LOW-DRAG BOAT

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-HULL ANGLES

$M = 0.80$



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FIGURE 16

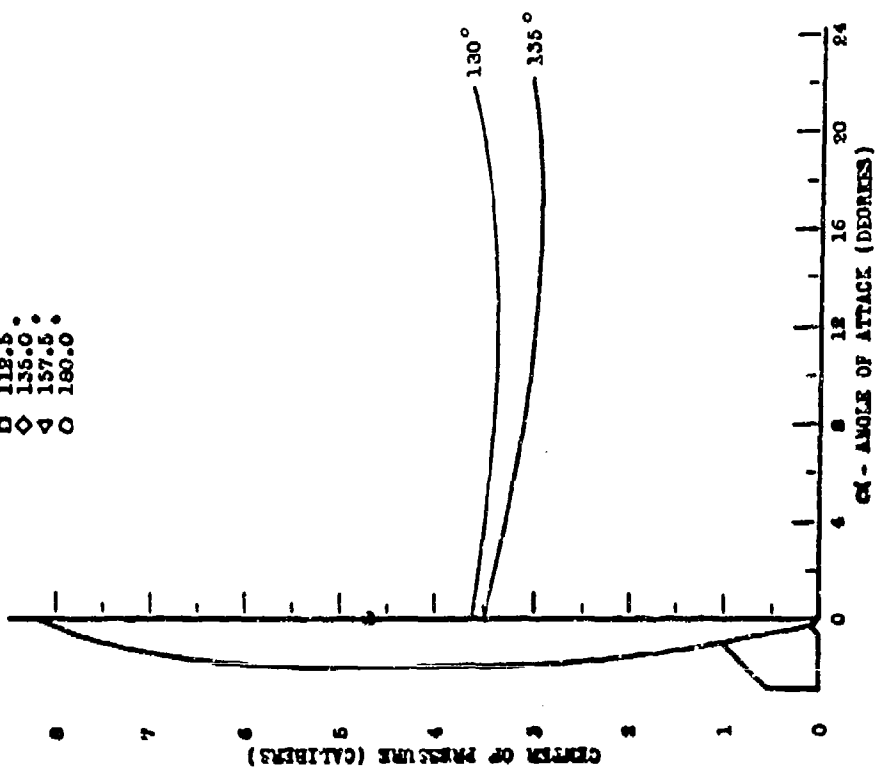
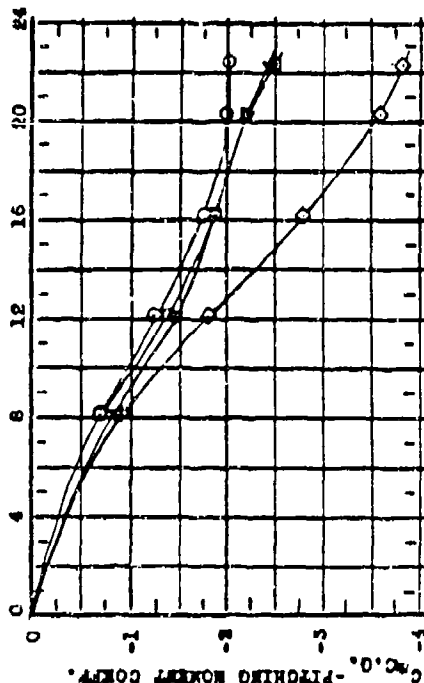
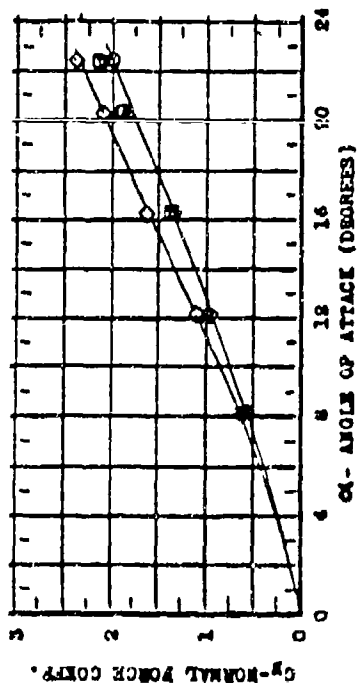
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LOW-DRAG BOXES

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 0.90$

θ
□ 112.5°
◇ 135.0°
△ 157.5°
○ 180.0°



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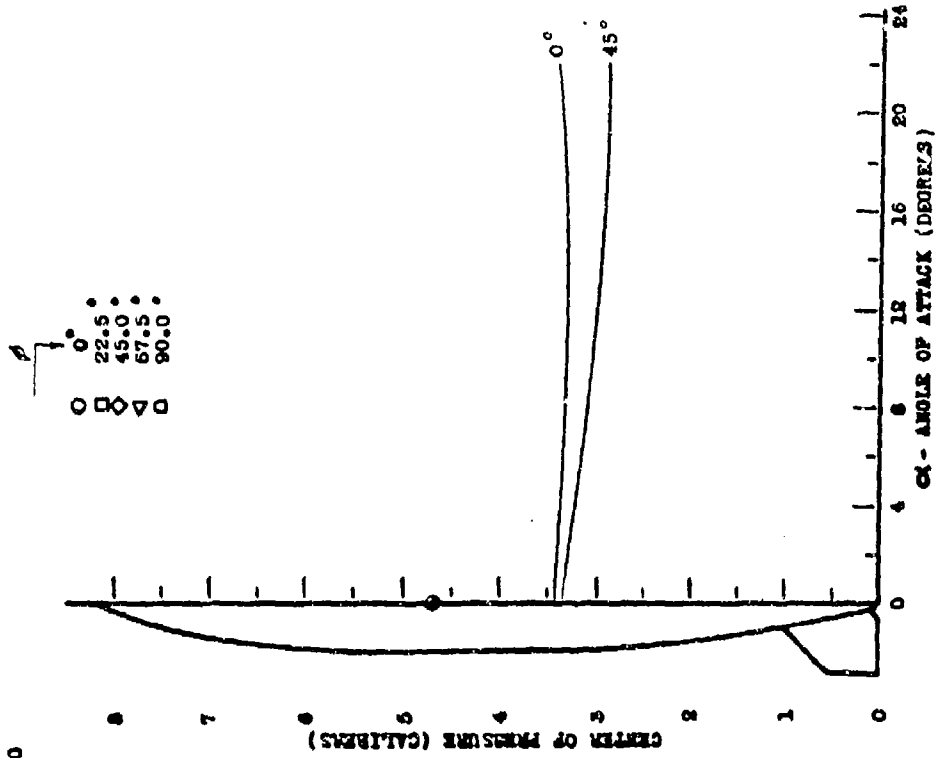
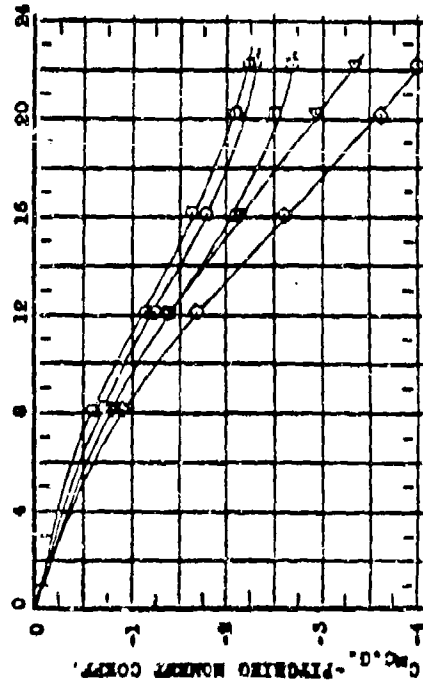
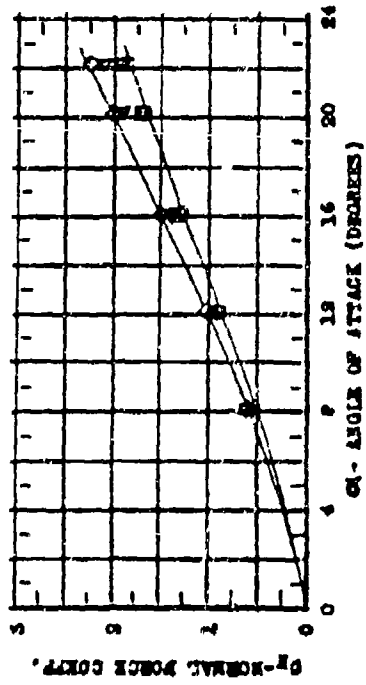
FIGURE 17

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LOW-DRAG BOMB

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 0.60$



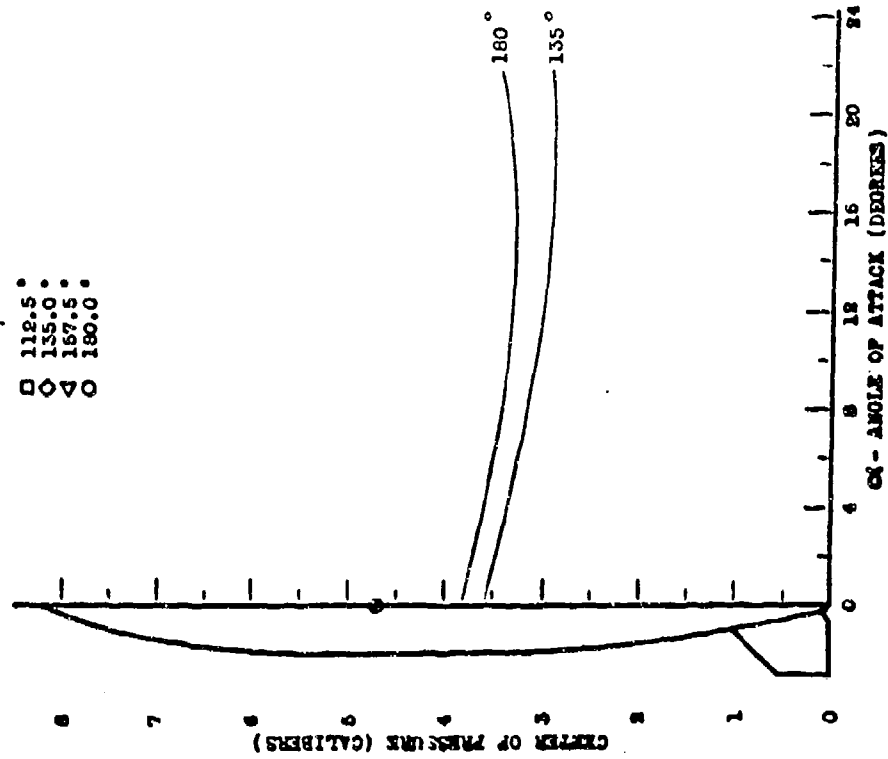
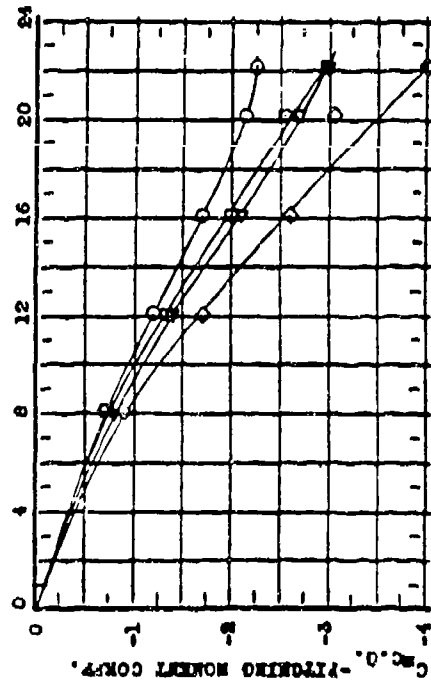
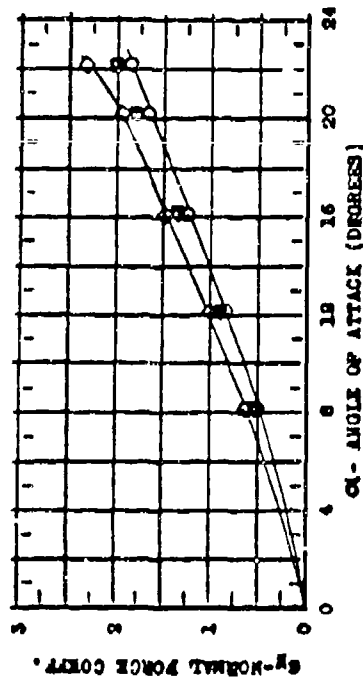
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FIGURE 18

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LOW-DRAG 2013

VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH ANGLE OF ATTACK
AT VARIOUS MODEL-ROLL ANGLES

$M = 0.60$



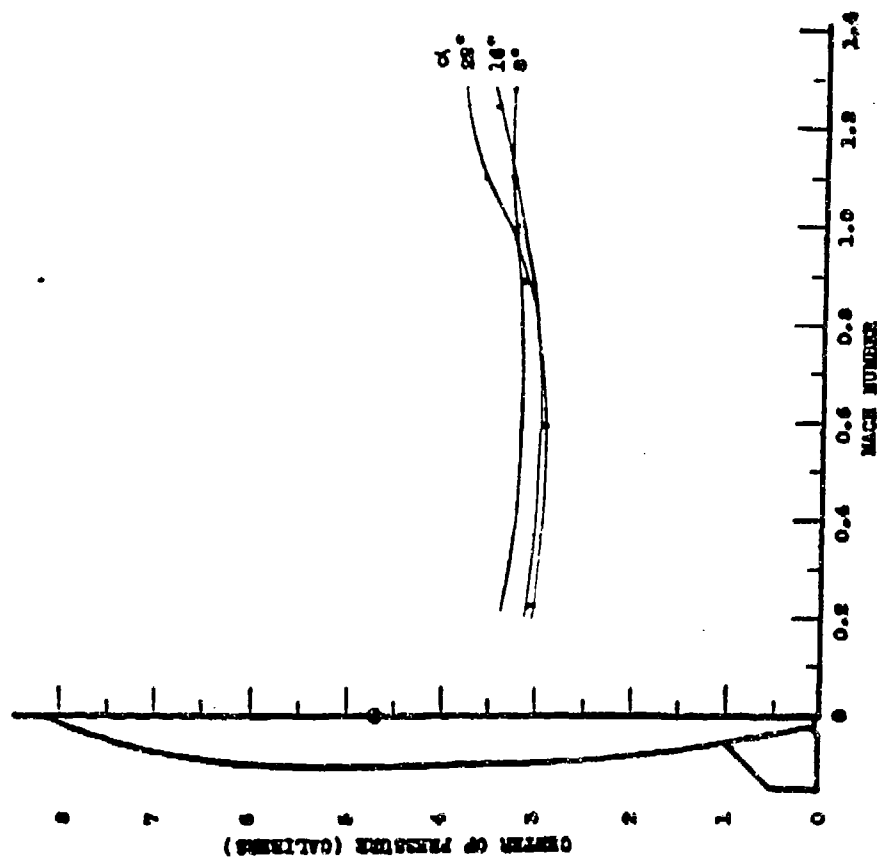
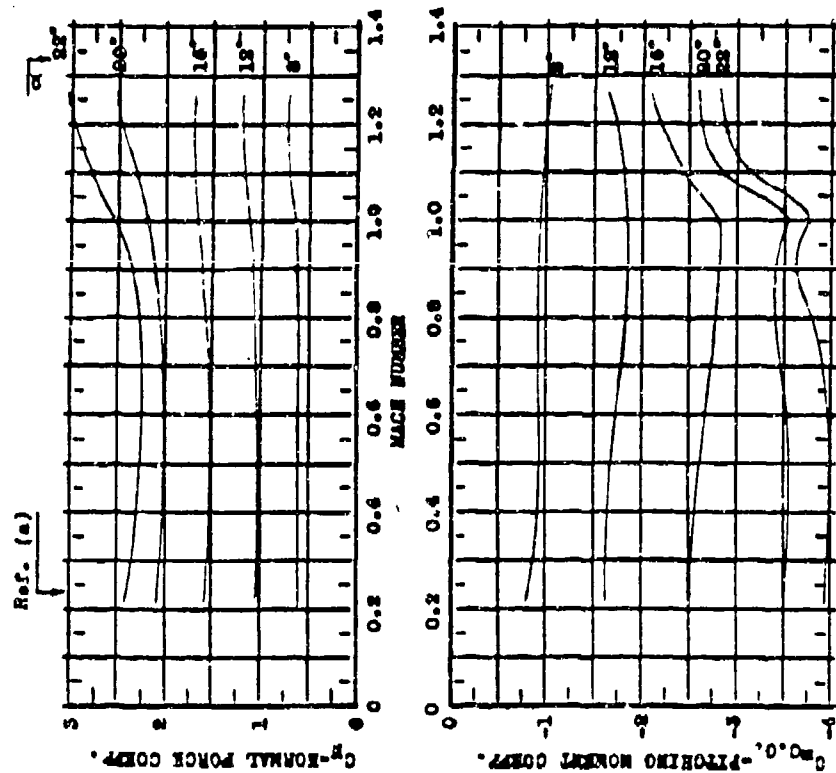
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FIGURE 19

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LOW-DRAO BOMB

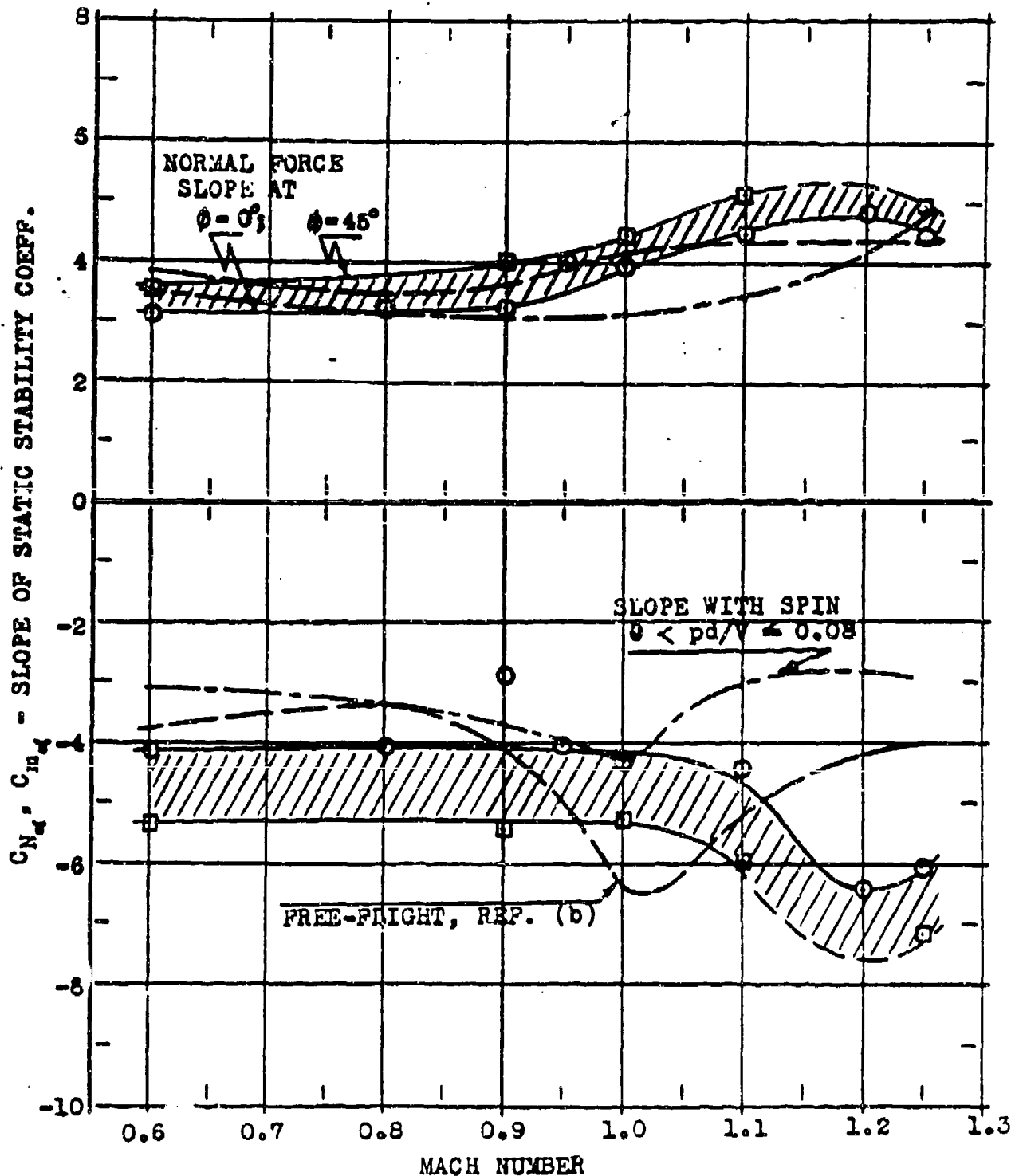
VARIATION OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT WITH MACH NUMBER AT $\beta=45^\circ$



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FIGURE 89

COMPARISON OF NORMAL FORCE AND PITCHING
MOMENT COEFFICIENT SLOPES FROM WIND TUNNEL
AND FREE-FLIGHT RANGE MEASUREMENTS



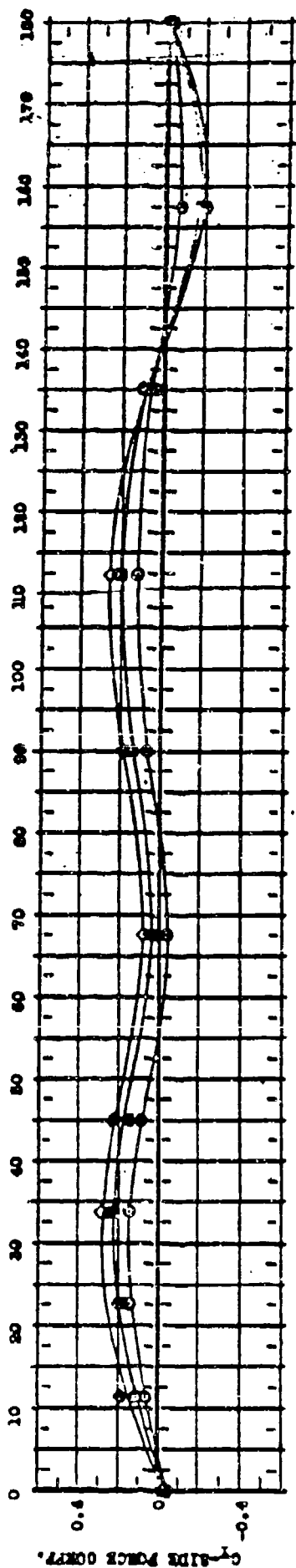
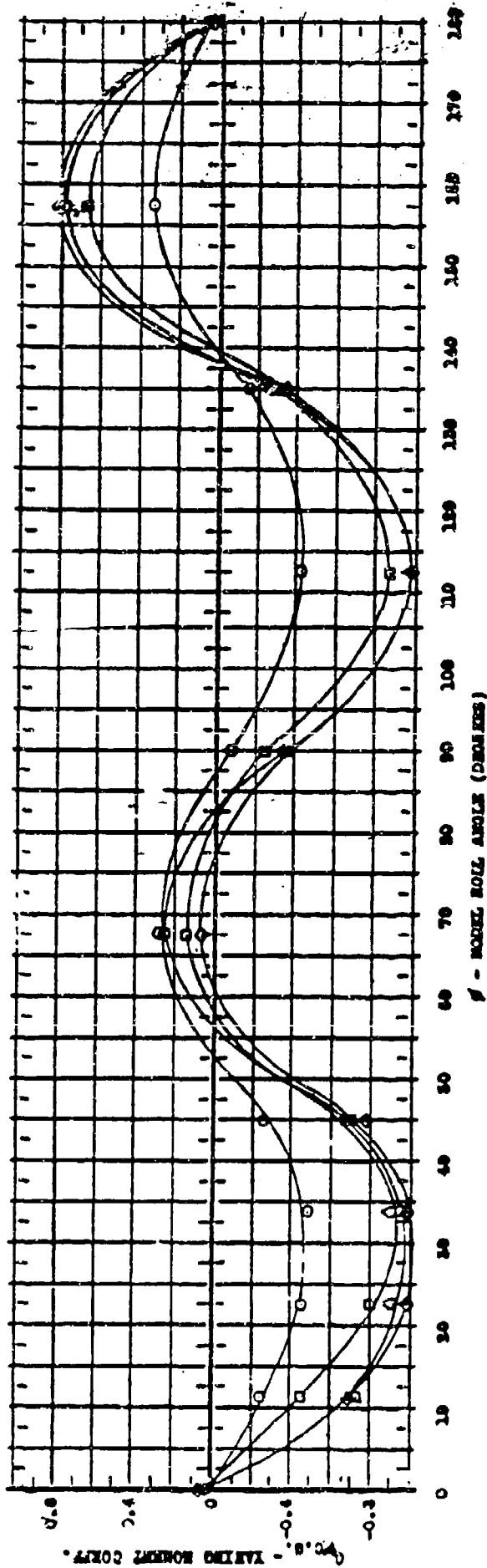
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LOW-DRAG BOMB

N-1,25

α
12°
16°
20°
22°

VARIATION OF SIDE FORCE AND YAWING
MOMENT COEFFICIENT WITH MODEL ROLL
ANGLE AT VARIOUS ANGLES OF ATTACK



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FIGURE 2

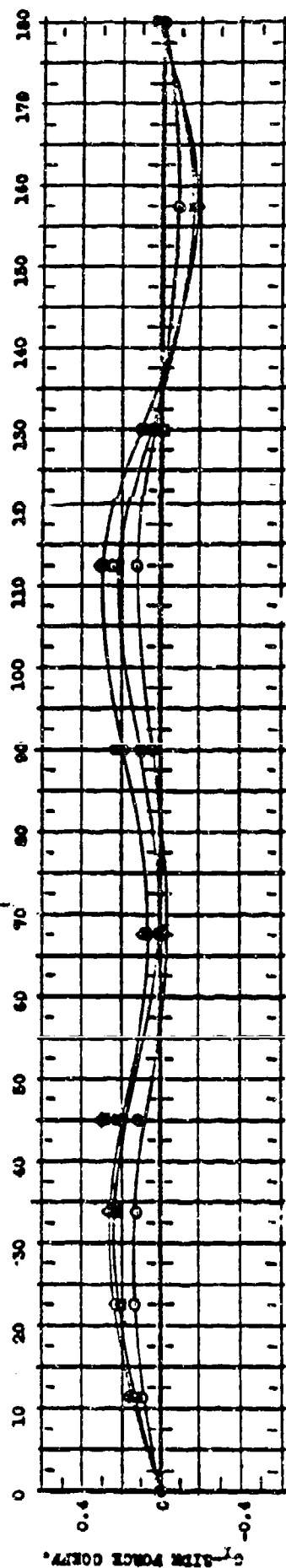
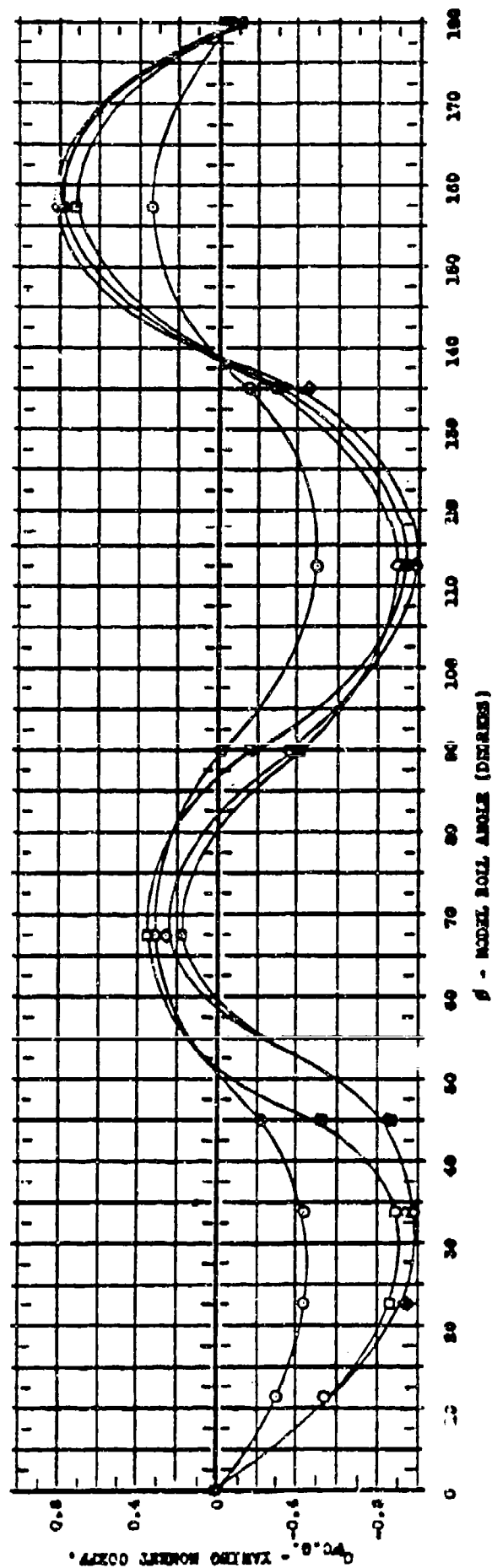
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LOW-SEAAG BONE

α
○ 12°
○ 16°
○ 20°
○ 22°

VARIATION OF SIDE FORCE AND YAWING
MOMENT COEFFICIENT WITH ROOT-ROLL
ANGLE AT VARIOUS ANGLES OF ATTACK

$M = 1.00$



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FIGURE 28

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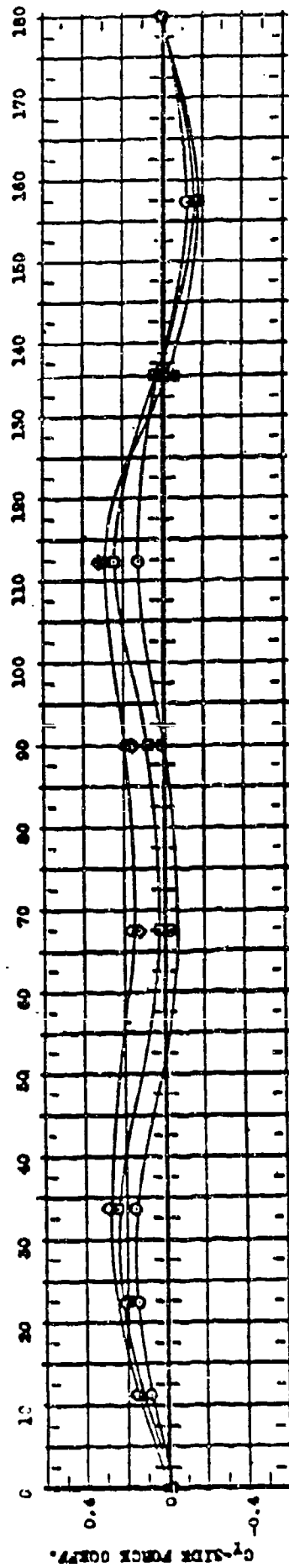
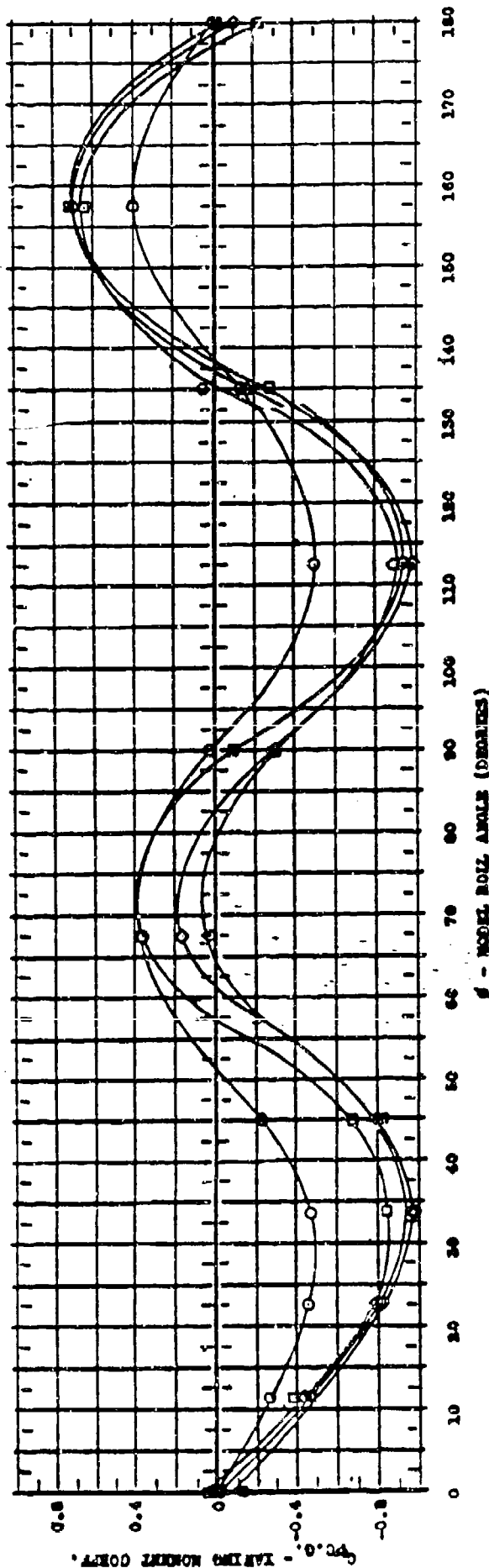
LOW-DRAW BOMB

VARIATION OF SIDE FORCE AND YAWING
MOMENT COEFFICIENT WITH MODEL ROLL
ANGLE AT VARIOUS ANGLES OF ATTACK

$M = 0.90$

α
12°
16°
20°
24°

○ □ ◇



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FIGURE 84

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LOW-DEAD BONE

VARIATION OF SIDE FORCE AND YAWING
MOMENT COEFFICIENT WITH MODEL ROLL
ANGLE AT VARIOUS ANGLES OF ATTACK

$M = 0.60$

α
12°
16°
20°
22°
○ □ ◇ ○

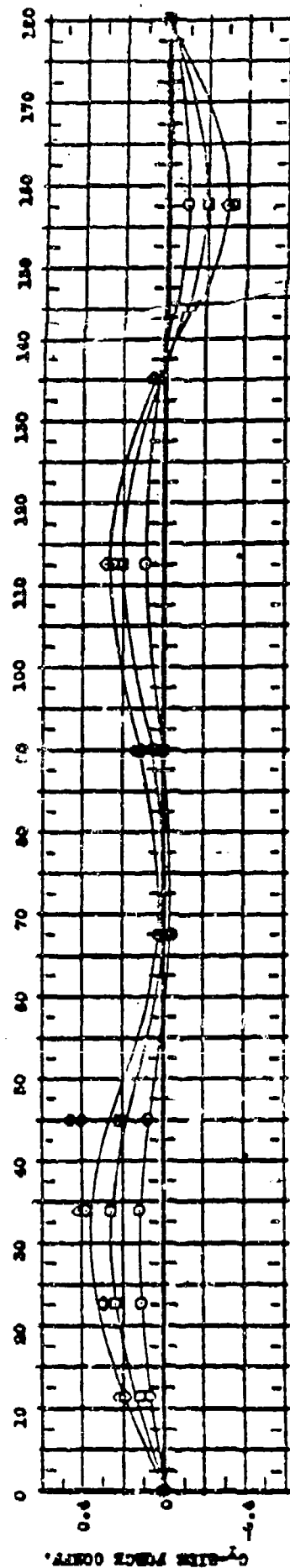
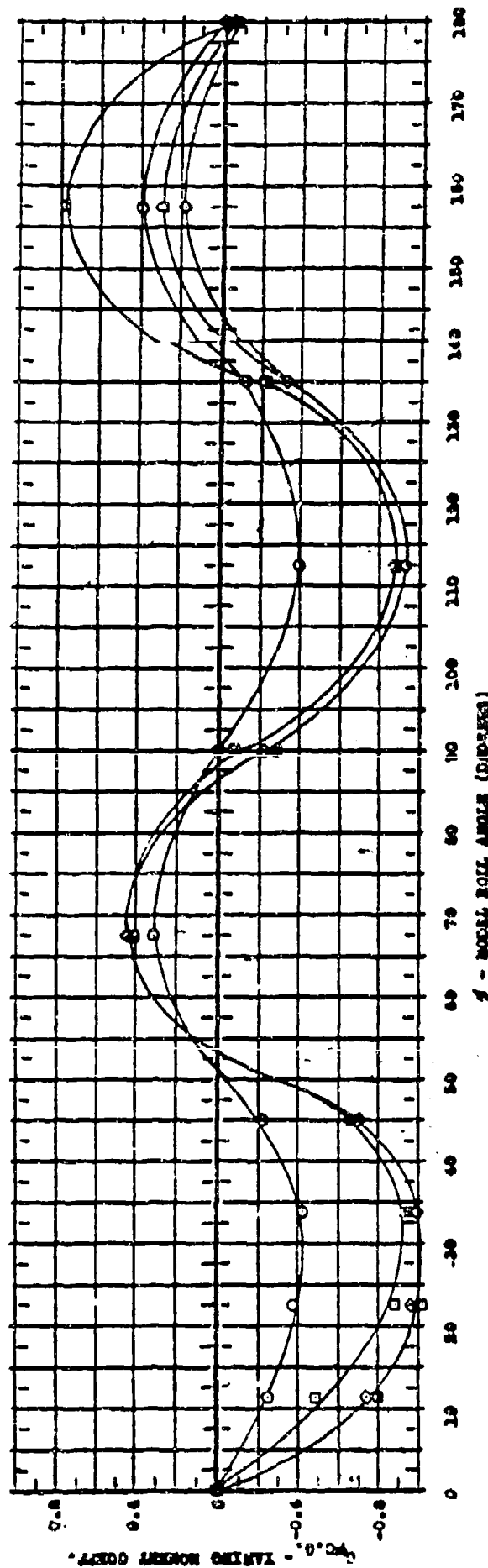


FIGURE 25

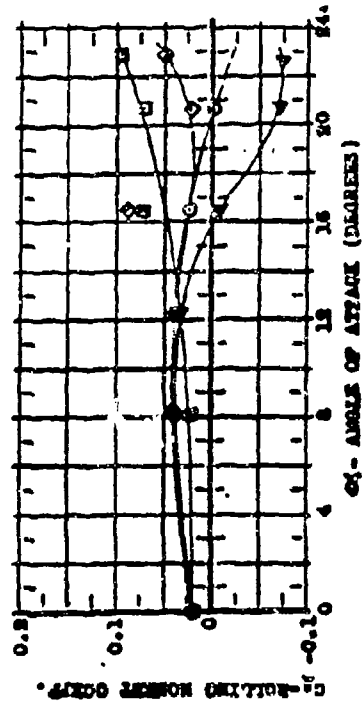
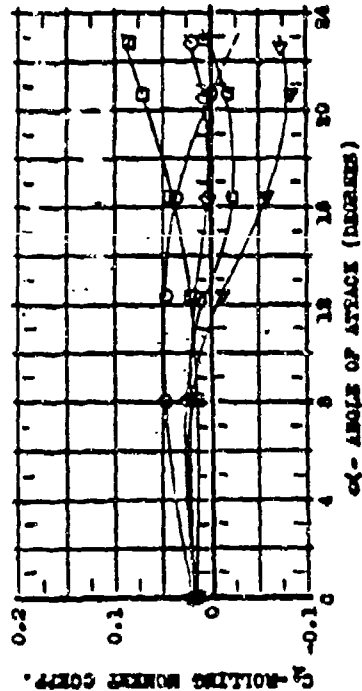
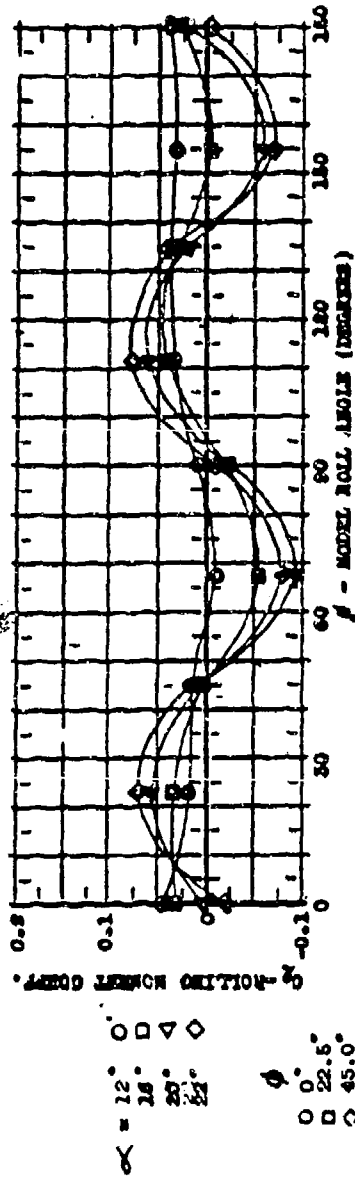
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LOW-DRAW NOSE

VARIATION OF ROLLING MOMENT COEFFICIENT
WITH ANGLE OF ATTACK AND MODEL ROLL ANGLE

M = 1.25



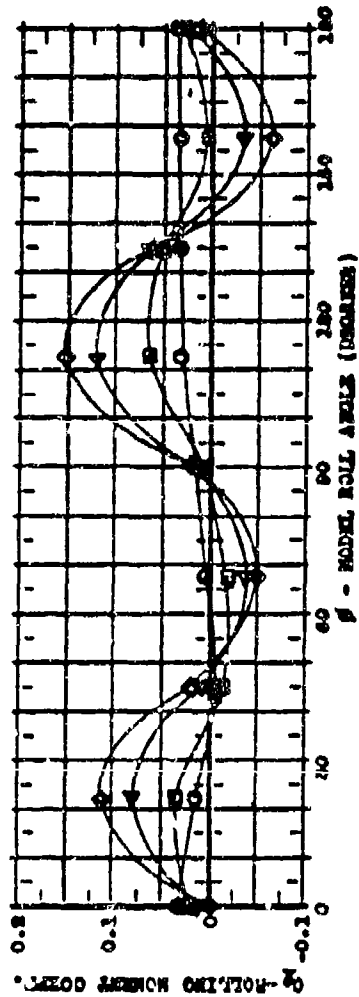
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LOW-DRAG BOMB

$M = 1.00$

VARIATION OF ROLLING MOMENT COEFFICIENT
WITH ANGLE OF ATTACK AND MODEL ROLL ANGLE

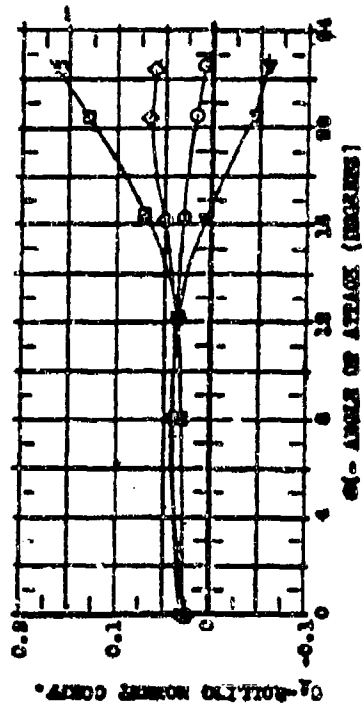
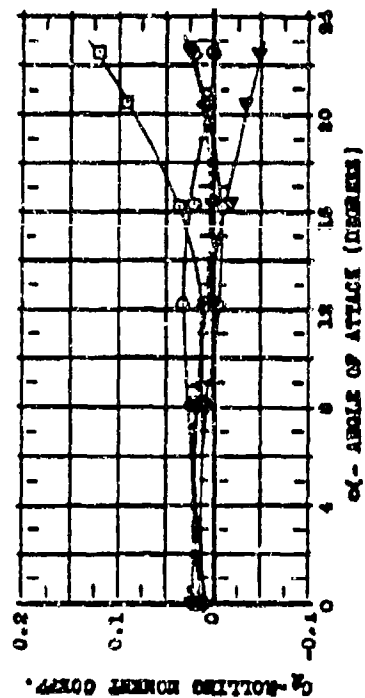


ϕ

- \circ 0°
- \square 22.5°
- \diamond 45.0°
- \triangle 67.5°
- \circ 90.0°

ϕ

- \square 112.5°
- \diamond 135.0°
- \triangle 157.5°
- \circ 180.0°



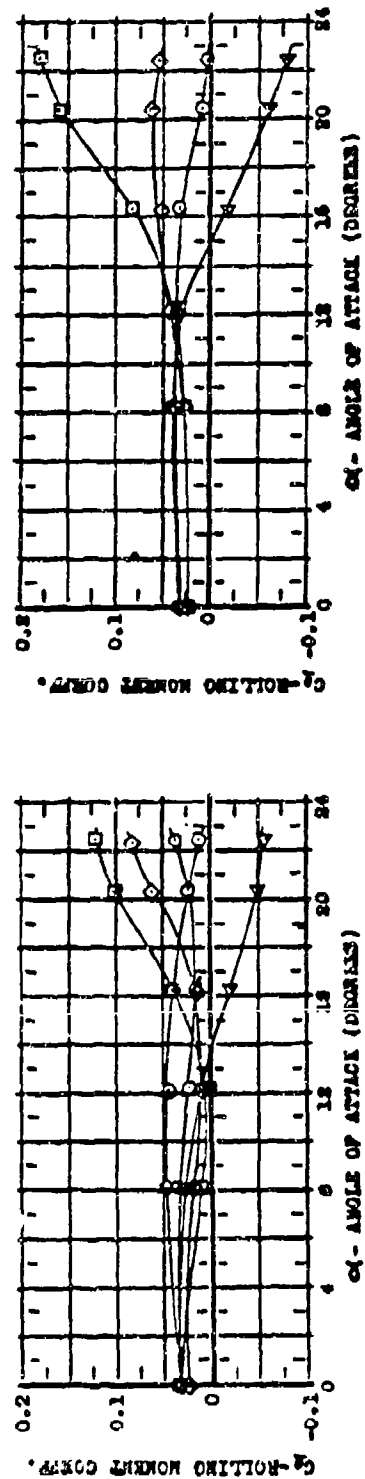
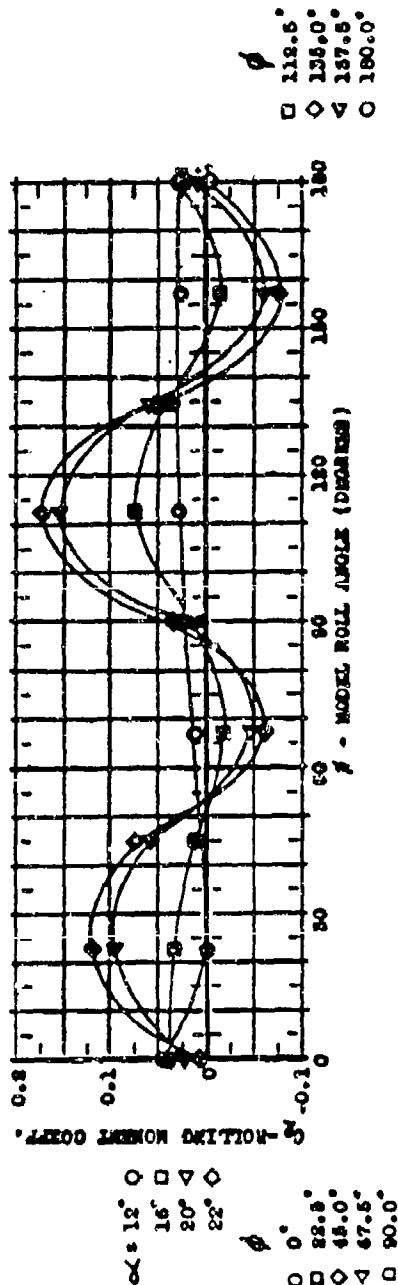
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LOW-DRAG BOMB

VARIATION OF ROLLING MOMENT COEFFICIENT
WITH ANGLE OF ATTACK AND MODEL ROLL ANGLE

$M = .90$



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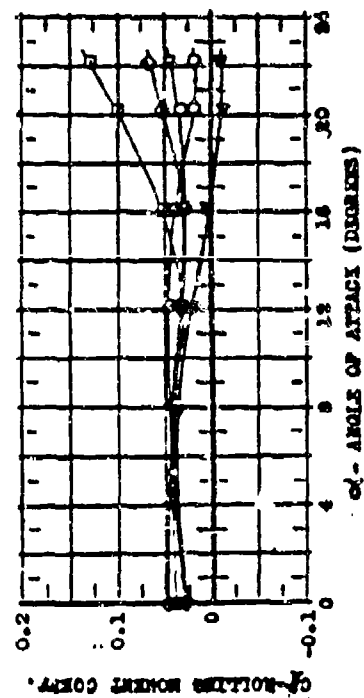
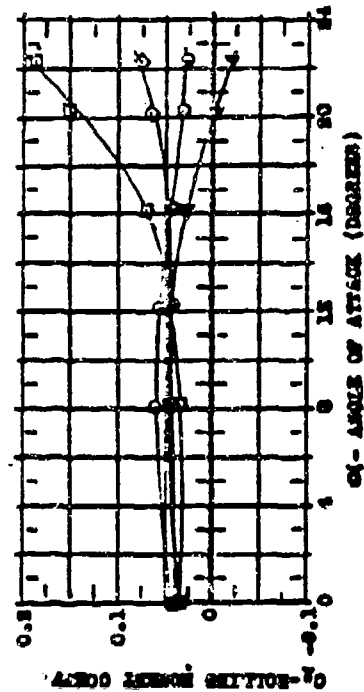
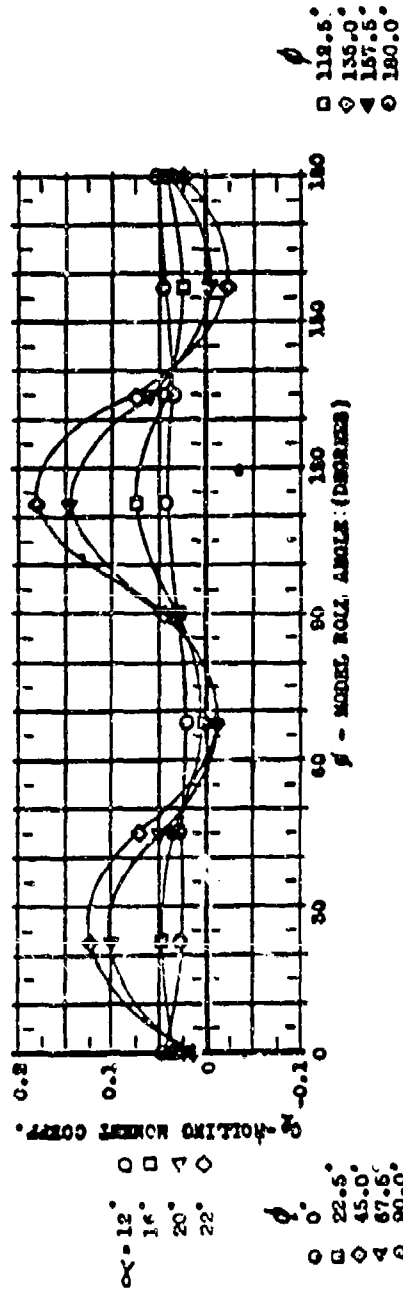
FIGURE 2

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LOW-DRAG ZONE

VARIAION OF ROLLING MOMENT COEFFICIENT
WITH ANGLE OF ATTACK AND MODEL ROLL ANGLE

M = .60



LOW-DRAG BOMB

VARIATION OF SPIN PARAMETER, $pd/2V$,
WITH ANGLE OF ATTACK AT VARIOUS
FREE-STREAM MACH NUMBERS

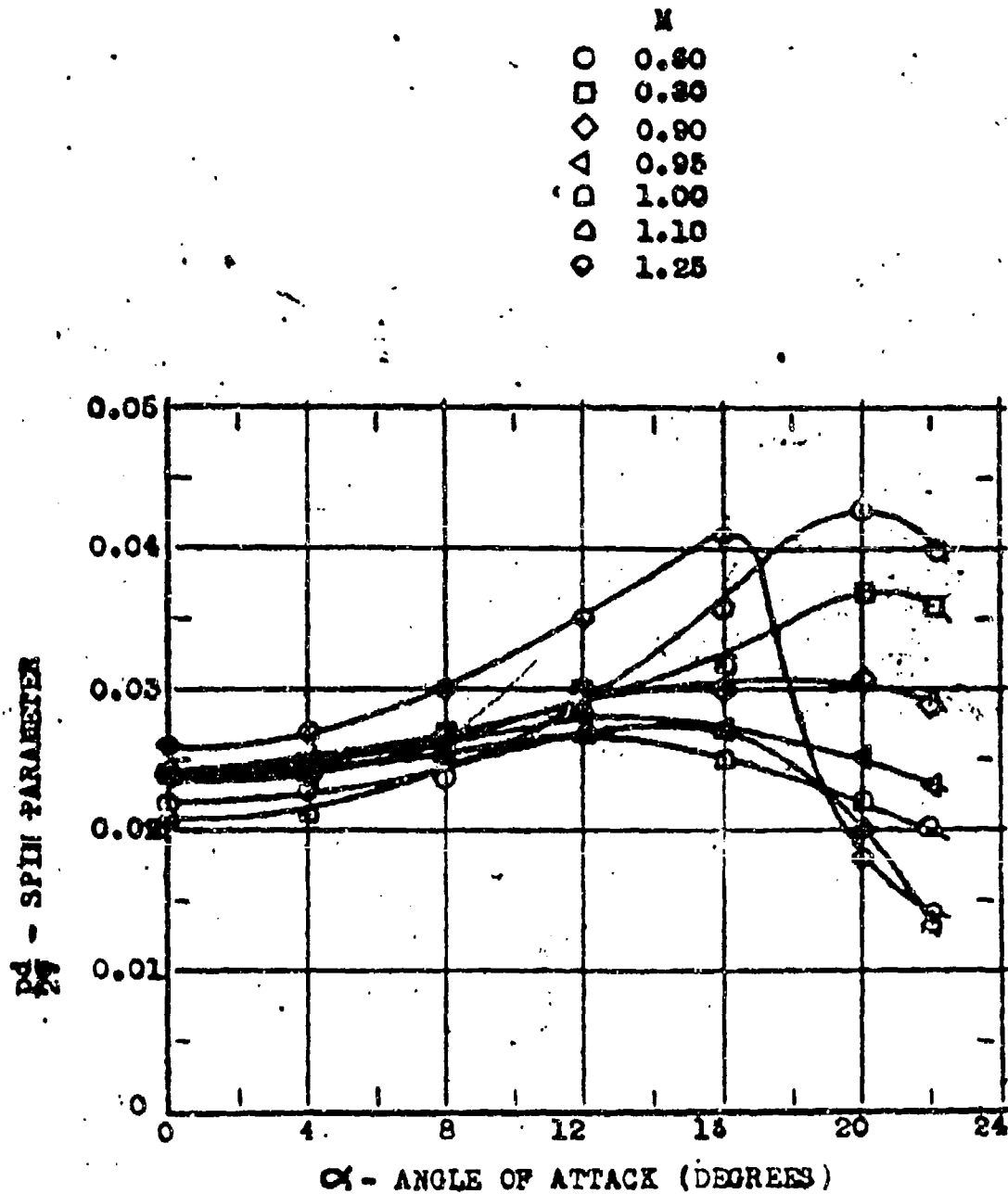


FIGURE 30

LOW-DRAG BOMB

VARIAION OF DRAG COEFFICIENT WITH
MACH NUMBER AT ZERO DEGREE ANGLE OF
ATTACK

○ $Re = 2 \times 10^6$, LUGS ON (BASE DRAG COMPONENT REMOVED)
 □ $Re = 2 \times 10^6$, LUGS OFF (BASE DRAG COMPONENT REMOVED)
 --- $1.52 \times 10^6 \leq Re \leq 3.45 \times 10^6$ (FREE-FLIGHT, REF (b))

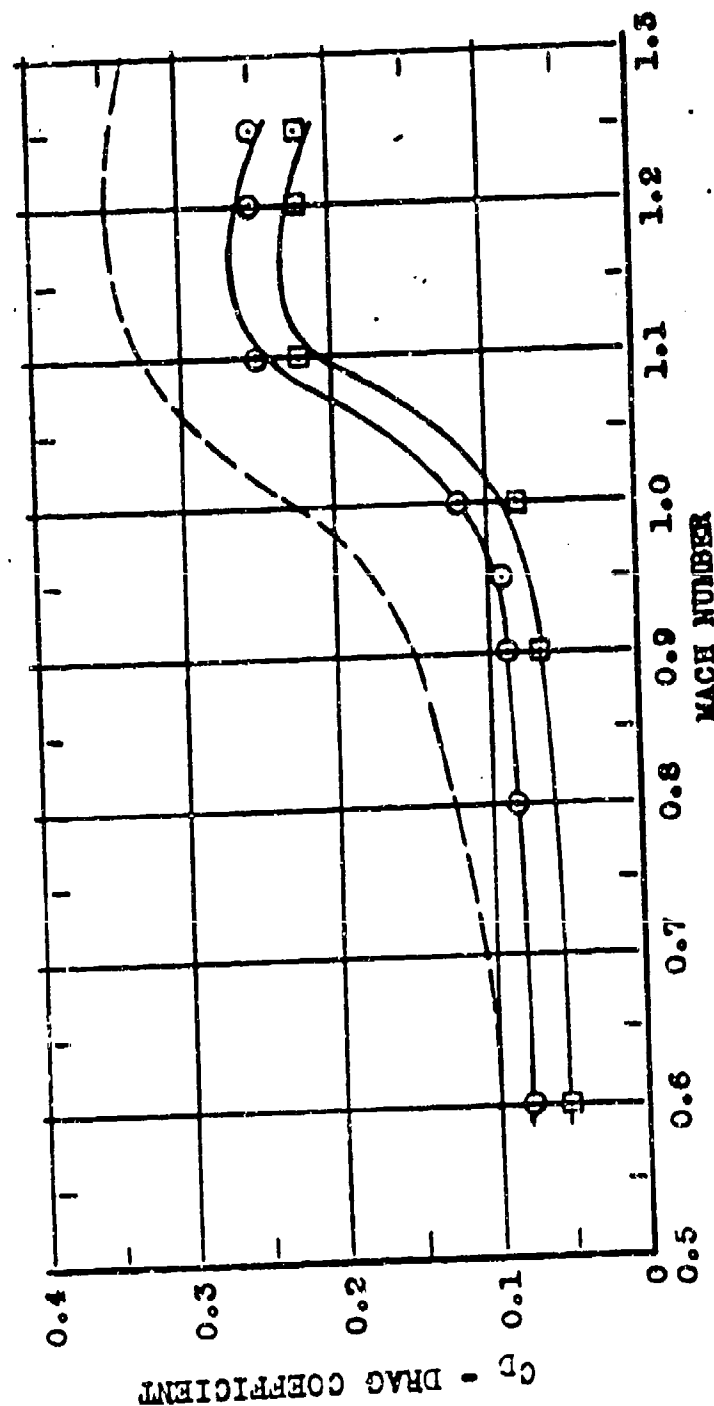


FIGURE 31

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